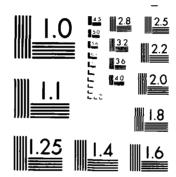
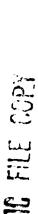
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NAVAL POSTGRADUATE SCHOOL Monterey, California





THESIS

CRITERIA FOR THE CLASSIFICATION
OF HYDROGRAPHIC POSITIONING DATA

bу

Nicholas E. Perugini September 1984

Thesis Advisor:

J. J. von Schwind

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The concept of presurvey positioning design is also presented. With the aid of computer graphic displays, the hydrographer can predict the accuracy of offshore positioning data prior to data acquisition. By analyzing accuracy lobes generated about shore stations, a survey can be designed to meet given specifications.

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Criteria for the Classification of Hydrographic Positioning Data

bу

Nicholas E. Perugini Lieutenant, National Cceanic and Atmospheric Administration B.S., Pennsylvania State University, 1976

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE IN HYDROGRAPHIC SCIENCES

from the

NAVAI POSTGRADUATE SCHOOL September 1984

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I. INTRODUCTION

A. EACKGROUND

A hydrographic record can be viewed as the resultant of two independent measurements made at a discrete point over a body of water. These measurements involve the determination of a vessel's position at a given time as well as the depth of water at that position. Of interest to the hydrographer and to the user of hydrographic data is the accuracy of the position determinations. Fundamental to the determination of positional accuracy is the identification of the sources of errors in position measurements and the ultimate treatment of these errors.

A hydrographic position can be determined by a number of methods all involving geometric relationships between known points and the vessel's unknown location. The known points may be fixed stations on shore, whose coordinates have been determined by geodetic survey methods, or they may be rapidly moving satellites whose coordinates in time and space can be defined very precisely. A hydrographic position is established by the intersection of two or more lines of position (LOP's) which are generated by the geometric relationships between the fixed points and the vessel's unknown location. The resultant accuracy of the vessel's position is therefore, in part, a function of the errors associated with the intersecting LOP's.

Several measures of accuracy can be used to evaluate the quality of a hydrographic position. Predictability, or absolute accuracy, is the measure of accuracy with which the positioning system can define the location of the same point in terms of geographic coordinates Repeatability, or

relative accuracy, is a measure with which a positioning system permits a user to return to a specific point on the earth's surface in terms of the LOP's generated by the system [Ref. 1, p. 14]. With the elimination of all systematic or hias errors, the terms repeatability and predictatility become identical. Hydrographic surveyors usually work toward this condition, although it is not always achievable.

Heinzen [Ref. 2] and Burt [Ref. 3] have presented several techniques for quantifying the repeatable accuracy for offshore positions. These techniques have roots in the statistical treatment of random error. Although the methods have been well documented, no single criterion to classify the accuracy of a hydrographic position has been agreed upon by the international hydrographic community.

Preceding the development of automation in hydrograph data acquisition and processing, the task of calculating accuracy figure to attach to each position in a hydrographic survey was unthinkable. To ensure overall accuracy in a survey, certain generalizations were developed to act as guidelines. For example, the U.S. Coast and Geodetic Survey https://dx.diago.org/hydrographic Manual [Sef. 4, p. 217] states the following concerning the strength of a three-point fix:

The fix is strong when the sum of the two angles is equal to or greater than 180° and neither angle is less than 30°. The nearer the angles equal each other the stronger will be the fix.

Generalizations of this type provided useful qualitative guidance for assuring a degree of positional accuracy and many are still in existence today.

With the aid of computers, the hydrographer now has the capacity to evaluate the accuracy of positioning data for an entire survey. An accuracy figure can be computed for each position in a survey and stored in a data base along with

cther survey information. This figure may provide useful information for users of the data, as well as a yardstick for the hydrographer to evaluate the quality of the work. Furthermore, a presurvey accuracy analysis enables a survey to be designed to meet desired specifications.

E. ACCURACY STANDARDS FOR HYDROGRAPHIC POSITIONING

In 1982, the International Hydrographic Organization (IHO) published new recommendations for error standards concerning the accuracy of hydrographic positions. These standards [Ref. 5] are:

The position of soundings, dangers and all other significant features should be determined with an accuracy such that any probable error, measured relative to shore control, shall seldom exceed twice the minimum plottable error at the scale of the survey (normally 1.0 mm on paper). It is most desireable that whenever positions are determined by the intersection of lines of position, three such lines be used. The angle between any pair should not be less than 300.

Most statisticiars define the term "probable error" as that error occurring at the 50 percent probability level. However, the author of the IHC standards, Commodore A.H. Cooper RAN (Ret.) has stated that the term "probable error" was interded to have no statistical significance. Munson interpreted the words "shall seldom exceed" to mean 10 percent of the time [Ref. 6]. Using this interpretation, the first sentence of the specification might be written:

The position of soundings, dangers and all other significant features should be determined with an accuracy such that any error in position measured relative to shore control will fall within a circle with radius of the firimum plottable error at the scale of the survey (normally 1.0 mm. on paper), with 90 percent confidence.

The specification in this form could be evaluated quantitatively. The criterion for defining accuracy in terms of a fixed probability is common in the field of surveying. For example, the standards of accuracy developed for geodetic

These errors are usually small in magnitude and can be eliminated by proper adjustment of the instrument by either the manufacturer or a qualified technician.

The field hydrographer has ultimate control over the geometric systematic errors associated with a theodolite. In range-azimuth positioning the theodolite and transmitter may occupy the same horizontal control station. If the theodolite is not set directly over the station a resultant systematic error will occur in all measurements. It can be shown that these errors are non-linear but do follow a mathematical relationship. Likewise, if the transmitter is not located directly over the station, a similar type of bias occurs. Depending on the eccentricity of the theodolite, the vessel's range from the theodolite, and the scale of the survey--these errors can seriously affect the absolute accuracy of the offshore positions.

In a similar fashion, it is also imperative to position the target directly over the horizontal control station used as an initial. Failure to do this will result in an error which will be propagated to offshore positions.

Many situations arise in the field where it is advantageous to set a transmitter and theodolite over a single horizontal control station. Frequently it is feasible to construct a platform to accommodate both instruments; in a case where it is not, the position of an eccentric horizontal control station near the original station should be determined and that station used for the location of one of the instruments. The theodolite and the transmitter then occupy two known stations and the geometric source of systematic error is eliminated.

b. Electronic Ranging Systems

The systematic errors associated with electronic positioning systems are complex in nature and functions of

2. Systematic Errors

Systematic errors occur with the same sign, usually of similar magnitude, and can be expressed in terms of a mathematical model. Systematic errors follow a defined pattern and occur in a number of consecutive related observations. Repetition of measurements does nothing to minimize their effect. In the case of hydrographic positioning, systematic errors are identified and modeled by calibration of the measuring instrument against a known standard. The following is a brief discussion concerning systematic errors and their treatment in relation to hydrographic positioning equipment.

a. Theodolites

In nearshcre surveys the theodolite is used primarily for range-azimuth and azimuth-azimuth positioning. Systematic errors associated with the theodolite can be classified into two groups: those associated with the physical design of the instrument and those involving the geometry of the positioning scheme. Some sources of systematic errors [Ref. 8] associated with the physical characteristics of a theodolite are:

- i. The horizontal circle may be eccentric.
- ii. Graduations on the horizontal circle may not be uniform.
- iii. The horizontal axis of the telescope (about which it rotates) may not be perpendicular to the vertical axis of the instrument.
- iv. The longitudinal axis of the telescope may not be normal to the horizontal axis.
 - v. The telescope axis and the axis of the leveling bubble may not be parallel.

range-azimuth fix. A range and an azimuth are generated from a known control station to the vessel's position. A second control station is used to fix the initial azimuth; a third shore control station is located 10 meters from the initial station and its coordinates are mistakenly used for the initial station in plotting. The resultant hydrographic position is in error, but this error will not be easily distinguished.

Although most blunders have their origin in human carelessness, some can be attributed to equipment malfunction. For example, microwave systems which generate IOF's are known to become unsteady under certain conditions. Spurious range readings resulting from signal reflections can be recorded as true positioning data. In this case, the blunder may or may not be easily detected.

In automated data acquisition systems, software has been developed to detect the occurrence of anomalous range readings. By inputting a course and speed of a vessel traveling along a line, the computer can determine if the recorded position is valid based on the principle of dead reckoning. If the recorded position is found to be invalid the hydrographer will be immediately alerted to the situation and can take action to remedy the problem. In non-automated systems the principle of dead reckoning is applied manually. Given the course and speed of the vessel, the validity of the position can be checked with spacing dividers. This involves checking the spacing between fixes recorded before and after the position in question.

Pefore any type of error analysis is to be performed on the hydrographic positioning data, it is essential that all blunders be identified and properly treated. In general, careful planning coupled with thorough checking will minimize the occurrence of blunders.

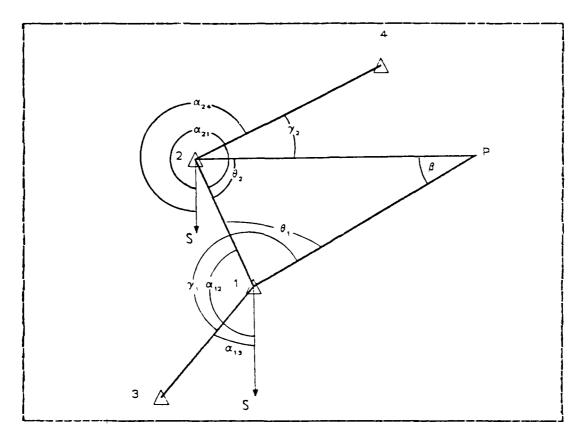


Figure 2.3 Geometry of an Azimuth-Azimuth Position

Consider the following as an example of a blunder associated with range-range geometry. An offshore position is to be determined by the intersection of two electronic IOP's generated from transmitters located on known shore stations. The vessel is working west of a shoreline that runs generally in a north-south direction. As the hydrographer faces the stations from sea, the southern shore station is mistakenly identified as left and the northern shore station as right. The resultant offshore position will plot to the east of the base line. This blunder is readily detected and can be easily remedied.

Not all types of blunders are so easily detected. Suppose an offshore position is to be determined by a

occupy stations 1 and 2, and initial on stations 3 and 4, respectively, the observer at station 1 measures angle γ_1 and the observer at station 2 measures γ_2 to the vessel. The angle of intersection, 8, is then computed by first determining the forward azimuths, measured clockwise from the south, from stations 1 to 2 (α_2), 1 to 3 (α_1), 2 to 1 (α_2), and 2 to 4 (α_2). The interior angles, 9 and 9, of triangle 12P are

$$\theta_{1} = |\alpha_{13} + \gamma_{1} - \alpha_{12}| \tag{2.3}$$

and

$$\theta_2 = |\alpha_1 + \gamma_2 - \alpha_1| \tag{2.9}$$

so the angle of intersection, $\boldsymbol{\beta}$, at the vessel's location is

$$\varepsilon = 180^{\circ} - (\theta_{1} + \theta_{2}) \tag{2.10}$$

E. CLASSES OF ERRORS

All hydrographic positioning measurements are subject to error. The following sections discuss categories of errors and methods used to treat these errors.

1. Elunders

Flunders are gross mistakes which are generally due to the carelessness of the observer. Blunders can vary in magnitude, ranging from large errors which are easily detected, to small errors which may be barely distinguished. They can be detected by making repeated observations or by carefully checking the data in the processing phase. Blunders occur in various forms and most can be avoided by carefully planning the data acquisition process.

in this arrangement but systems employing a laser can also be used for short-range work. Another LOP is generated by fixing an azimuth from a shore control station to the vessel. A second control station is used for an initial azimuth by the observer. Azimuth determinations can be made after observing directions with a theodolite as an observer tracks the moving vessel.

There are two ways to determine a range-azimuth position. The most common way is to have the theodolite and the transmitter occupy the same shore control station. Hence, the angle of intersection, β , of the LOP's is always 90°. This arrangement is commonly used by the National Ccean Service (NOS) for large-scale nearshore surveys.

The other way is to have the theodolite and the transmitter occupy two different control points. Then the geometry is similar to that of the range-range position. The angle of intersection, β , is computed by trigonometric relationships among the azimuth of a line between the shore stations, the observed direction to the vessel, and the measured range to the vessel.

4. Azimuth-Azimuth

Azimuth-azimuth positioning geometry is used for nearshore high-accuracy surveying. Theodolites are set over two control stations on shore. The vessel is sighted on simultaneously by the two theodolite observers, generating two visual IOP's whose intersection define the vessel's location. Initial azimuths are fixed by sighting on control stations which are visible to the observers.

The angle of intersection for an azimuth-azimuth position is dependent on the geometric relationships between the occupied stations, the initial stations, and vessel's position (Fig. 2.3). Assuming that theodolite observers

where the term $1/\sin{(\alpha/2)}$ is called the lane expansion factor. The angle of intersection ,8, between the two hyperbolas is then given by

$$\beta = \frac{\alpha_r + \alpha_g}{2} \tag{2.7}$$

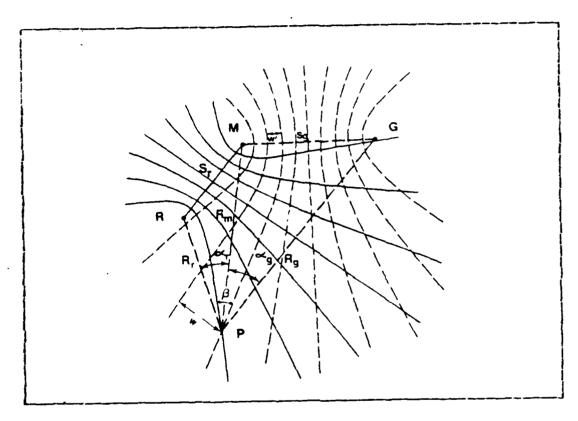


Figure 2.2 Geometry of a Hyperbolic-Hyperbolic Position

3. Range-Azimuth

This positioning geometry is used for nearshcre, line-cf-sight surveys. One LOF is generated by an electronic range originating from a transmitter located on a shore control station. A microwave system is commonly used

Hyperbolic location methods can be divided into two groups based on the electronic principles used to define the distance differences [Ref. 7, p. 87]. Loran is an example of a pulse system in which the differences in times cf arrival of pulses transmitted by the master-slave combinations are translated into distance differences. The resultant position has no lane ambiguity and is easily resolved. The second method of hyperbolic positioning involves measuring a phase difference from two master-slave combinations at the vessel's position. The phase difference translates into a fractional lane count which in itself provides an ambiguous position. This ambiguity is resolved by using a whole-lane counter which is initialized at a known geographical point. In hyperbolic positioning, the ship is in a passive mode and the system can be used by many vessels.

The angle of intersection between the two hyperbolas can be computed by first defining the following quantities:

S is the length of red base line,

S is the length of green base line,

R is the distance between master and vessel's position P,

 R_r is the distance from red slave to point P,

 R_{g} is the distance from green slave to point P,

 α is the angle between lines PM and PR, and

a is the angle between lines PM and PG.

The spacing between lanes increases with distance from the master-slave pair. The lane widths along the base line are

$$w'_r = \frac{\lambda_r}{2}$$
 and $w'_g = \frac{\lambda_g}{2}$ (2.5)

Then the lane widths at any point P are

$$w_r = \frac{\lambda_r}{2} \left(\frac{1}{\sin (\alpha_r/2)} \right) \quad \text{and} \quad w_g = \frac{\lambda_g}{2} \left(\frac{1}{\sin (\alpha_g/2)} \right) \quad (2.6)$$

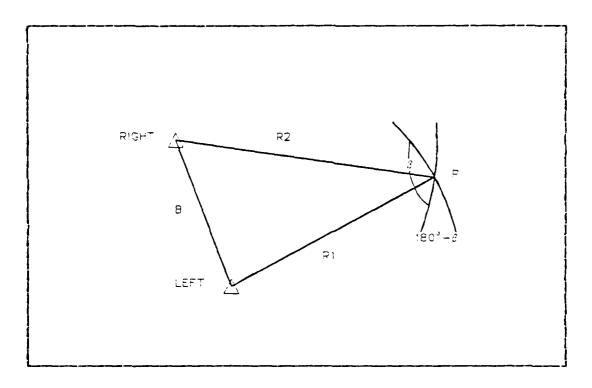


Figure 2.1 Geometry of a Range-Range Position

2. Hyperbolic-Hyrerbolic

Hydrographic positioning by hyperbolic-hyperbolic geometry utilizes the intersection of two hyperbolas each generated about a pair of shore control stations. A hyperbola is the locus of points in which the difference of distance from two fixed points is always constant. A three-station hyperbolic net is the most commonly used hyperbolic mode for offshore survey (Fig. 2.2). One family of hyperbolas (Red) are generated about a master station, M, and a slave, R; while a second family of hyperbolas (Green) are generated with respect to the master and a second slave, G. For the first family of hyperbolas, the control points M and R act as the foci, while points M and G act as the foci for the second family.

problem of lane ambiguity must be addressed. Ranges are expressed in full and partial lane counts where a lane width w is

$$w = \frac{\lambda}{2} \tag{2.2}$$

where λ is the wavelength of the transmitting frequency, f, and given by

$$\lambda = \frac{\mathbf{c}}{f} \tag{2.3}$$

Medium-range systems commonly in use today are Cubic Western's "ARGO," Hasting Raydist's "Raydist," and Odom Cffshcre's "Hydrotrack."

The angle of intersection associated with a rangerange position is computed from a simple trigonometric relationship. The vessel's position P (Fig. 2.1) is determined by the intersection of the ranges from the left and right shore stations, R1 and R2 respectively. B is the base line distance computed between the two known shore stations. Since the range circles from the shore stations intersect at two points, it is necessary for the plotter to recognize which side of the base line the vessel is on in order to eliminate the ambiguity. The angle of intersection of the two LOP's (B) is given by the law of cosines

$$\beta = 180^{\circ} - Arc \cos \left(\frac{B^2 - R1^2 - R2^2}{2 R1 R2} \right)$$
 (2.4)

In qualitative terms, the fix is strongest when ß approaches 90°. Most hydrographic specifications limit the angle of intersection from a minimum of 30° to a maximum of 150°.

An electronic positioning system may be active or passive. In an active system, a transmitter from the survey launch keys the transmission of ranges from the shore station. In turn, the signals generated from the shore stations (slaves) are then received by the launch. An active system is limited to a finite number of users, usually not more than about four. The number of users of a passive system is unlimited as the survey launch requires only a receiver which is constantly listening for signals which are being transmitted from shore.

Short-range, or line-of-sight, positioning systems are used for nearshore hydrographic surveys. These systems operate in the microwave region of the electromagnetic spectrum (3 to 10 GHz). A distance is determined by observing the time needed for a pulse to travel from a master transponder located aboard the survey vessel to a remote transponder on shore and back to the master transponder.

Knowing the average velocity of the electromagnetic pulse, the distance D is ther

$$D = \frac{c \cdot t}{2} \tag{2.1}$$

where c is the group velocity of the wave packet and t is the two-way travel time. Short-range systems which are in wide use today are Racal Decca's "Trisponder" and Motorcla's "Mini-Ranger." These systems have direct range readout and are readily interfaced into a navigational computer and a data acquisition system. Both systems are active and user limited.

Medium-range positioning systems operate in the 1to 5-MHz frequency range of the electromagnetic spectrum. A distance is determined by measuring the phase relationship tetween transmitted and received waves. These systems are usually referred to as continuous wave systems and the

II. NATURE OF THE PROBLEM

The development of an accuracy figure for offshore positions is inherently tied to the geometry of the positioning method and the errors which are associated with the positioning equipment that is used. This chapter will discuss the geometric and statistical elements involved in determining an offshore position and presents several methods for quantifying repeatable accuracy.

A. HYDROGRAPHIC POSITIONING GEOMETRIES

An offshore fix can be determined by the intersection of two or more LOP's. These LOP's may be generated by electronic or visual means. Working toward the development of an accuracy index, it will be necessary to compute the angle of intersection of the LOP's associated with different positioning geometries. The following sections discuss the geometry of conventional offshore positioning methods and ways to compute the angles of intersection. This thesis will not address the geometry involved in a three-point sextant fix.

1. Range-Range

Establishing an offshore fix by range-range geometry involves measuring distances electronically from fixed positions on shore to the vessel's unknown location. Ranges can be determined by measuring the elapsed time between transmission and receipt of a radio pulse or by comparing the phase of the transmitted wave with the phase of the received wave [Ref. 2]. In each case, transmitters are set on stations on shore whose coordinates are determined by precise land survey methods.

method of classification is a useful index for quantifying the accuracy of positions. The computed radii of the 90 percent confidence circles can serve as an accuracy figure that can be attached to each position in a survey and stored in a data base.

The third objective of this thesis is to demonstrate that a presurvey analysis can be used in designing positional accuracy to meet specifications. The existing general guidelines for planning can be better defined. For example, in planning a survey hydrographers usually lay out circles which delimit the 30° and 150° boundaries that define the minimum and maximum allowable intersection angles between two LOP's. As a means to meet accuracy requirements, it can be shown that these limits should vary based on the scale of the survey and the precision of the positioning equipment.

control surveys have their origin in probability theory. Procedures for obtaining first-order geodetic positions require sixteen repeated theodolite observations of each direction. Lower order positions require fewer numbers of observations. Given the precision of one observation of each direction, it can be demonstrated that increasing the number of observations coincides with increasing the probability of the direction falling within specified limits.

Regarding accuracy determinations, there are several problems unique to hydrographic surveying. Whereas standards for other types of surveys rely on multiple observations of the same quantity, the accuracy of a hydrographic position must be evaluated in terms of a single observation (which may be the intersection of two or more LOP's). Diverse methods for obtaining a hydrographic position exist and these methods must all be evaluated using the same criterion. Also, there is a broad spectrum of equipment used in hydrographic positioning and in many cases the precision of this equipment is not well defined.

C. CEJECTIVES

A need exists to give quantitative meaning to the accuracy specifications set forth by the IHO. One of the objectives of this thesis is to demonstrate that defining the specifications in terms of the fixed 90 percent confidence level is a valid interpretation. By defining what the specifications imply, procedures can be developed to meet the standards.

A second objective of this thesis is to apply the theory of errors, associated with hydrographic positioning, to a data set. This analysis involves classifying positioning data acquired in a survey based on the radii of circles of equivalent probability. It will be demonstrated that this

many variables. Munson [Ref. 9, p. 4] addresses several problems associated with short-range systems used in hydrographic surveys. The most common problems with short-range systems are variation in range and calibration drift with time. Variations in internal equipment time delays in the transmitter, the transponder, or the receiver can induce errors in measured ranges. For pulse systems such variations can occur due to temperature dependence of components and fluctuations in signal strength at the transponder. Multipath effects are also a problem. Under some circumstances a reflected wave and the directly transmitted wave arrive with a phase difference of 180°. Cancellation or fading of the directly transmitted signal can result.

NOS conducts base line calibrations of shortrange positioning systems periodically during the course of
a survey to minimize or eliminate systematic error. In this
process, a transmitter and receiver are each placed over
control stations on shore and the measured range is compared
to the true range. In this way the systematic error is
eliminated by zeroing the instrument or by applying a
constant correction to raw data. System checks are
performed daily to assure there is no drift from the original calibration. A check can be accomplished by comparing
a position defined by the ranging system to a known fixedpoint position, to a sextant fix position, or an intersection position.

Munson [Ref. 9, p. 5] also discusses sources of systematic errors associated with medium-range systems. The most significant systematic errors occur as a function of position due to varying propagation velocity. The medium-range electronic signal propagation velocity depends on the surface conductivity and transmission path (over water, over land, or over different types of land). Because of this dependence, systematic errors as a function of position

cccur at different effective phase velocities. Knowing the propagation velocity to use, or the phase correction to make as a function of range, is a problem. Sky wave and storm interference also pose problems. At extreme ranges of operation, sky wave interference can affect the more predictable ground wave, especially during nighttime operations. Lane ambiguities are also a problem. Most systems are inherently ambiguous and must be zero set and continually monitored for lane jumps or loss of signal which results in the loss of lane count.

NOS uses several techniques to determine the systematic error associated with medium-range positioning systems. These techniques involve determining a whole and partial lane count for phase comparison systems. Two of the more widely used techniques are comparison of three-point sextant fix positions to positions determined by the electronic ranging system and calibration of the electronic system at a fixed point. In both techniques the whole lane counts are fixed by the calibration; correctors to the partial lane count are determined and applied to the raw ranging data.

3. Random Errors

Random errors are chance errors, unpredictable in magnitude or sign, and are governed by the laws of probability [Ref. 10, p. 1206]. They are errors which remain after blunders and systematic errors have been removed. Random errors result from accidental and unknown combinations of causes and are beyond the control of the observer. Greenwalt [Ref. 12, p. 2] states they are characterized by:

- i. Variation in sign; positive errors occur with equal frequency as negative ones.
- ii. Small errors cccur more frequently than large errors.
- iii. Extremely large errors rarely occur.

Random errors are unique to specific types of positioning equipment and vary in magnitude depending on the precision of the instruments that are used. The following section cutlines statistical methods for their treatment.

C. TREATMENT OF RANDOM ERRORS.

1. Cne-Dimensional Errors

Certain basic statistical quantities must first be defined in the analysis of random errors. Consider a vessel moored securely to a fixed offshore platform. A number of ranges, n, from a microwave transmitter located on a shore control station are recorded. The mean of these observations is

$$\mu_{X} = \sum_{j=1}^{n} \frac{x_{j}}{n}$$
 (2.11)

where x represents an individual observation. The standard error, s, of the observations is then

$$s = \sqrt{\frac{1}{n-1}} \sum_{j=1}^{n} (x_j - \mu_X)^2$$
 (2. 12)

where the quantity $(x_1^-\mu_x^-)$ is referred to as the residual, or true error, v_1^- , of a particular observation. As n gets very large, the factor 1/n can be substituted for 1/(n-1) in Equation 2.12. Likewise, in treating the large sample, σ can be substituted for s and μ for μ_x^- , where μ and σ are the mean and standard error of the entire population.

It is of interest to determine the probability of cccurrence of a particular observation. The normal cr Gaussian distribution equation relates the residual of a particular random variable with the probability of its

cccurrence, and is given by

$$P(v) = \frac{1}{\sigma \sqrt{2\pi}} e^{-(\frac{v^2}{2\sigma^2})}$$
 (2.13)

The plot of this equation yields the normal distribution curve (Fig. 2.4). The height of the curve above the vertical axis is proportional to the probability of a particular error occurring.

The probability of a residual falling between any two residuals v and v can be computed by integrating Equation 2.13 as

$$P(v) = \int_{V_{2}}^{V_{1}} \frac{1}{\sigma \sqrt{2\pi}} e^{-(\frac{v^{2}}{2\sigma^{2}})} dv$$
 (2.14)

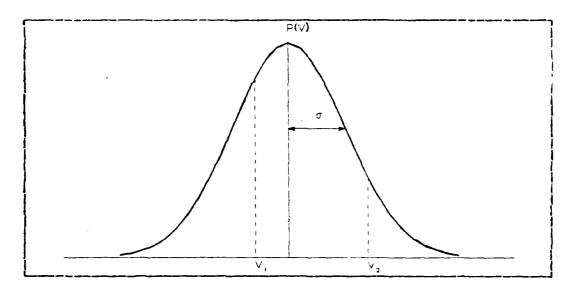


Figure 2.4 The Normal Distribution

This integral is difficult to evaluate analytically so tables have been compiled to aid in computations. For $v_1 = +\sigma$ and $v_2 = -\sigma$, it can be shown that P(v) = 0.6827. In other words, the probability that a particular observation will fall within \pm 1 σ of the mean is 68.27 percent.

Feturning to the example of the vessel moored to the cffshcre platform, the mean and the standard error for the observations are easily computed. With this information and Equation 2.14, the probability of a range error falling within specified limits can be computed. Conversely, by fixing a probability, the associated limits of the range error can be computed. In statistical terms, a particular observation will fall within specified limits with a certain confidence.

Actual values of one-dimensional standard errors for hydrographic positioning equipment are a subject of debate betweer manufacturers and users. Some manufacturers of microwave positioning equipment claim standard errors of ±1 meter. On the other hand, Munson [Ref. 9, p. 6] states that microwave systems demonstrate accuracies of 3 meters at short ranges but show larger errors at ranges of 15 km and greater. NOS assumes a 3-meter standard error in all of its short-range accuracy computations. It is apparent that further study is needed to adequately define the nature of errors associated with electronic positioning equipment.

Waltz [Ref. 13] performed an extensive study to determine the pointing error of a Wild T-2 theodolite. His results showed that the pointing error associated with this instrument under hydrographic survey conditions was about 1.3 meters and was independent of distance.

2. Iwo-Dimensional Errors

The intent of this paper is to apply statistical methods developed by others to a hydrographic data set containing two-dimensional errors which are defined by two random variables. Lengthly and complex derivations are not presented. Burt [Ref. 3] and Heinzen [Ref. 2] show adequate derivations of formulas associated with two-dimensional errors and can be referenced for full details.

The following assumptions are made concerning two-dimensional errors associated with intersecting LOP's:

- i. The random errors of each LOP are normally distributed.
- ii. Systematic or hias errors have been removed from the observations.
- iii. The intersecting LOP's are coplanar.
- iv. The error LOF's are parallel to the exact LOF's.

In developing a usable mathematical model for accuracy determinations, the four assumptions hold to a high degree for all hydrographic positioning geometries.

Consider again the vessel moored to a fixed cffshcre platform. Assume two ranges are measured from two different shore control stations at the same time and that the range readings are uncorrelated. The observation of this pair of ranges is repeated many times. After a large number of observations, the means and standard errors of the individual ranges are determined. Suppose the mean ranges, or the actual LOP's, intersect at an angle of 90° and that the computed standard errors are equal $(\sigma = \sigma)$. If each data pair (x_1, y_1) is plotted, the spread of points about the mean coordinates results in a circular cluster (Fig. 2.5). A higher density of points occurs near the intersection of the mean ranges and the density of points decreases outward from the intersection of the mean ranges.

In this special case, which is called a circular normal distribution, the probability of a point falling within a specified radius, R, from the intersection of the mean ranges is

$$P(R) = 1 - e$$
 (2.15)

where $\sigma_1 = \sigma_2 = \frac{\sigma_c}{c}$ and is defined as the circular standard error. Using Equation 2.15, R can be computed by fixing P(R), or conversly, F(R) can be computed by fixing R. Letting R = $\sigma_1 = \sigma_2 = \sigma_3$, then P(R) = 0.3935. In other words, 39.35 percent of all errors in a circular normal distribution are not expected to exceed the circular standard error [Ref. 12, pp. 25-26].

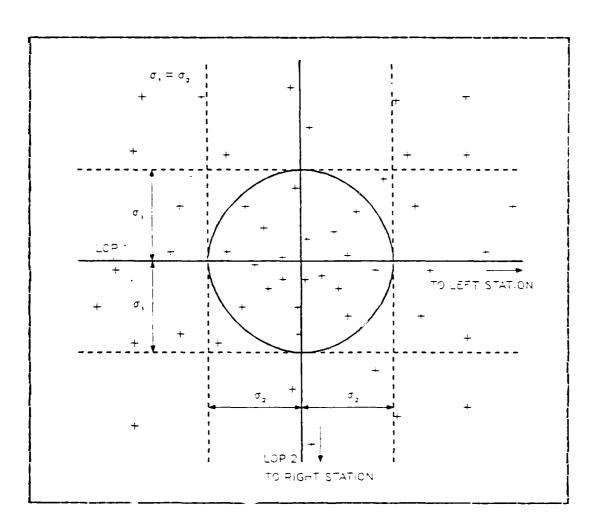


Figure 2.5 Circular Normal Distribution

In the case where the two uncorrelated LCP's intersect at an angle other than 90° or $\sigma_1 \not= \sigma_2$, the contours of

equal density are ellipses centered about the point defined by the intersecting ICP's (Fig. 2.6). The two-dimensional probability density function becomes [Ref. 1, p. 136]

$$P(v_x, v_y) = \frac{1}{2\pi\sigma_x\sigma_y} e$$
 (2.16)

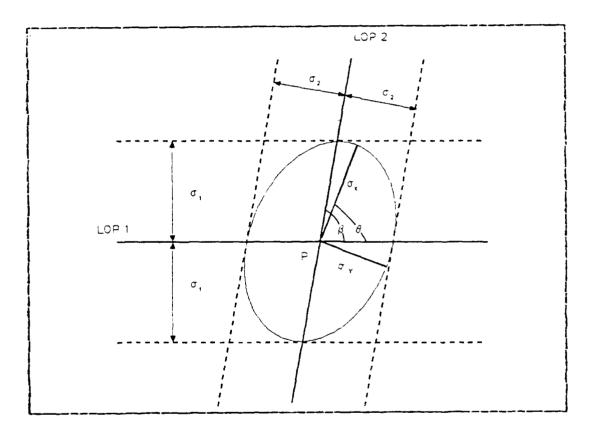


Figure 2.6 Error Ellipse Formed by Two Uncorrelated LCP's

where

 $\mathbf{v}_{\mathbf{x}}$ is the residual in the direction of the semi-major axis of the error ellipse,

 $\mathbf{v}_{\mathbf{y}}$ is the residual in the direction of the semi-minor axis,

 $\boldsymbol{\sigma}_{\mathbf{x}}$ is the standard error in the direction of the semimajor axis,

 $\boldsymbol{\sigma}_{\boldsymbol{y}}$ is the standard error in the direction of the semi-minor axis,

and

$$K^{2} = \frac{v_{X}^{2}}{\sigma_{X}^{2}} + \frac{v_{Y}^{2}}{\sigma_{Y}^{2}}$$
 (2.17)

The sclution of Equation 2.16 with values of K for different P's yields the results in Table I [Ref. 12, p. 23]. For a 39.35 percent probability, the axes of the ellipse are 1.0000 σ and 1.0000 σ ; for a 50 percent probability, the axes are 1.1774 σ and 1.1774 σ .

	T A	BLE	I	
Values	of	the	Constant	K

PROPABILITY	<u>K</u>
390% 300% 300% 300% 300% 300% 300% 300%	1.0000 1.1774 1.4142 2.1460 3.0349 3.5000

The error ellipse can be used for accuracy computations by developing relationships for σ and σ in terms of the initial information σ , σ , and β . Bowditch [Ref. 10, p. 1213] gives the following equations for independent IOP's relating these quantities:

$$\sigma_{x}^{2} = \frac{1}{2\sin^{2}\beta} \left\{ \sigma_{1}^{2} + \sigma_{2}^{2} + \sqrt{(\sigma_{1}^{2} + \sigma_{2}^{2})^{2} - 4\sin^{2}\beta \sigma_{1}^{2}\sigma_{2}^{2}} \right\}$$
 (2.18)

and

$$\sigma_y^2 = \frac{1}{2\sin^2\beta} \left\{ \sigma_1^2 + \sigma_2^2 - \sqrt{(\sigma_1^2 + \sigma_2^2)^2 - 4\sin^2\beta \sigma_1^2\sigma_2^2} \right\}$$
 (2.19)

In these equations, g is assumed to be the acute angle between the LOP's.

In certain special cases, the above equations take on more manageable forms. In range-range and azimuthazimuth positioning it is often assumed that $\sigma_i = \sigma_i = \sigma_i$ Equations 2.18 and 2.19 then reduce to

$$\sigma_{x} = \frac{\sqrt{2}}{2\sin(\frac{1}{2}\beta)} \sigma \qquad (2.20)$$

and

$$\sigma_{y} = \frac{\sqrt{2}}{2\cos(\frac{1}{2}\beta)} \sigma \qquad (2.21)$$

In the concentric range-azimuth case, σ # σ , and β equals 90°. Equations 2.18 and 2.19 then simplify to

$$\sigma_{\mathbf{x}} = \sigma_{\mathbf{1}} \tag{2.22}$$

an i

$$\sigma_{y} = \sigma_{2} \tag{2.23}$$

where σ > σ and σ > σ . The case for correlated LOP's is more complex. The calculation of $\sigma_{\mathbf{x}}$ and $\sigma_{\mathbf{v}}$ involves a coordinate transformation from a linear skewed coordinate system to an uncorrelated rectargular coordinate system. The following discussion is taken from Heinzen [Ref. 2, pp. 49-53].

Assume a hydrographic position is established by the intersection of two correlated LOP's (Fig. 2.7a). LOP 1 and

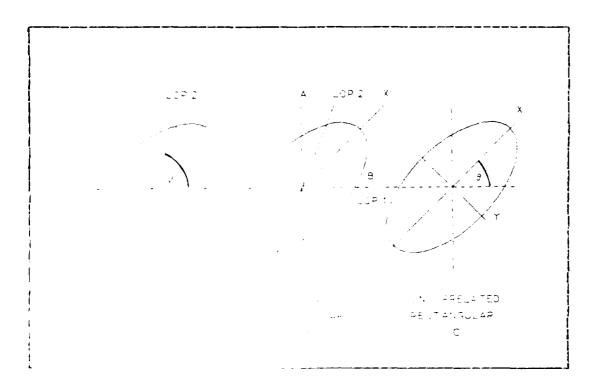


Figure ... Transformations for Correlated IOP's

If Positive the contrast excess in the skewed coordinate system, with the semi-major and semi-mire access in the error ellipse are not coincident with the skewed coordinate system axes. The correlation coefficient between the two LOP's is ρ . Assume σ > σ .

The standard errors and correlation coefficient in a correlated rectangular coordinate system with axes A and B must now be determined. A coordinate transformation from the skewed system to the correlated rectangular system must be made yielding the standard errors along the new coordinate axes (Fig. 2.7b)

$$\sigma_a^2 = \frac{1}{\sin^2 \beta} \left(\sigma_1^2 + 2\rho_{12} \sigma_1 \sigma_2 \cos \beta + \sigma_2^2 \right) - \sigma_2^2$$
 (2-24)

and

$$\sigma_b = \sigma_2 \tag{2.25}$$

The correlation coefficient in the correlated rectangular system is

$$\rho_{ab} = \left(\frac{\sigma_2}{\sigma_1} \cos \beta + \rho_{12}\right) \left\{1 + \rho_{12} \left(\frac{\sigma_2}{\sigma_1}\right) \cos \beta + \left(\frac{\sigma_2}{\sigma_1}\right) \cos^2 \beta\right\}^{-\frac{1}{2}}$$
 (2.26)

To determine $\sigma_{\mathbf{x}}$ and $\sigma_{\mathbf{y}}$, a second coordinate transformation must be performed from the correlated rectangular system to an uncorrelated rectangular system with axes X and Y (Fig. 2.7c). The semi-major and semi-minor axes of the error ellipse are then

$$\sigma_{x} = \sqrt{\frac{\sigma_{a}^{2} + \sigma_{b}^{2}}{2}} \sqrt{1 + \sqrt{1 - \frac{4\sigma_{a}^{2}\sigma_{b}^{2}(1 - \rho_{ab}^{2})}{(\sigma_{a}^{2} + \sigma_{b}^{2})^{2}}}}$$
 (2-27)

an i

$$\sigma_{y} = \sqrt{\sigma_{a}^{2} + \sigma_{b}^{2} - \sigma_{x}^{2}}$$
 (2.28)

When $o_{12} = 0$, these equations become identical to the simplified versions in Bowditch [Ref. 10].

The orientation of the semi-major and semi-minor axes relative to the intersecting LOP's is the third parameter which fixes the error ellipse. The angle 9 (Figs. 2.6 and 2.7) is measured counter-clockwise from LOP 1 to the semi-major axis of the error ellipse [Ref. 11] and is given by

$$\theta = \frac{1}{2} \arctan \left\{ \frac{\sigma_1^2 \sin(2\beta) + 2\rho_1 \sigma_1 \sigma_2 \sin(\beta)}{\sigma_1^2 \cos(2\beta) + 2\rho_1 \sigma_1 \sigma_2 \cos(\beta) + \sigma_2^2} \right\}$$
(2-29)

For the special case of $\sigma_1 = \sigma_2$ and $\rho_{12} = 0$,

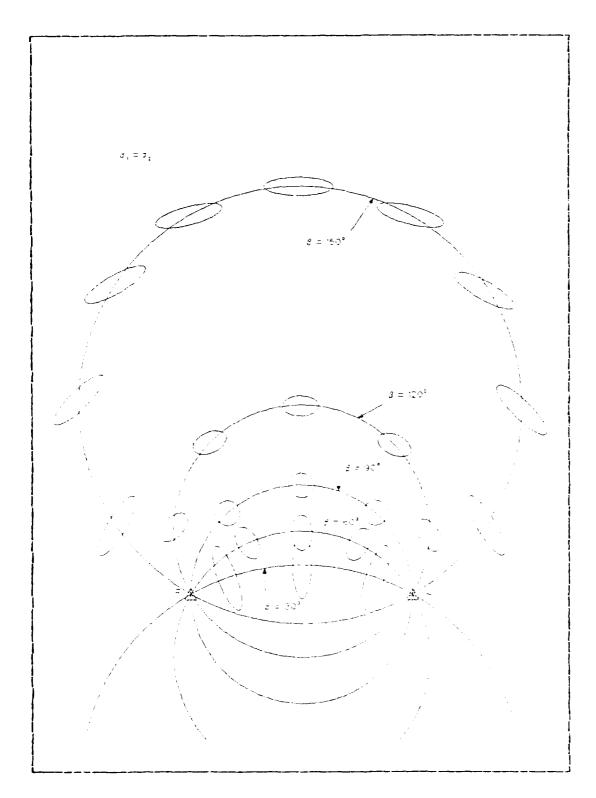
$$\theta = \frac{8}{2} \tag{2.30}$$

The orientation of the error ellipse in an orthogonal ccordinate system can be represented by adding or subtracting g to the orientation of LOP 1. Care must be taken on determining the quadrant of the outcome. As a general rule, the error ellipse always lies within the acute angles formed by the intersecting LOP's.

The orientation and dimensions of the error ellipse provide a useful index for evaluating the accuracy of a hydrographic position. Its greatest attribute is that it accurately represents the error distribution about the intersection of two ICP's in terms of a fixed probability. It is interesting to examine the variation in the relative dimensions and orientations of error ellipses as they vary in a range-range configuration with $\sigma = \sigma = \sigma$ (Fig. 2.8). The dimersions of the ellipses are specified by Equations 2.20 and 2.21 and $\sigma_{\mathbf{x}}$ and $\sigma_{\mathbf{y}}$ are functions of β only for fixed σ . Therefore, the dimensions of the ellipses remain constant along a contour of constant g; only the orientation changes. A line of constant B is a circle which includes stations L and F. Note that the dimensions of the ellipses for β 's of 30° and 150° are identical. The ellipses about the 90° angle of intersection contour are circles and represent the strongest possible positions in this scheme. With varying B's, the directional nature of the distribution can be noted.

3. Circular Precision Indexes

Although the error ellipse gives a true representation of the error distribution about a hydrographic position, its use has certain drawbacks. The characteristics of the ellipse must be secified by the three quantities $\sigma_{\mathbf{x}}$, $\sigma_{\mathbf{y}}$, and a. A single figure for evaluating the positional accuracy cannot be used. Greenwalt [Ref. 12, p. 26] states that when $\sigma_{\mathbf{x}}$ and $\sigma_{\mathbf{y}}$ are not equal, a circular error



Pigure 2.8 Error Ellipses Around a Range-Range System

TABLE V
Coordinates of Control Stations

STATICN NAME	GECLETIC CCORD.	MIM COORD.	
USE MON	36° 36° 04.685° 121° 52° 35.900°	N W	Y = 1982.43 m. $X = 4853.36 r.$
MUSSEL	36° 37' 18.151" 121° 54' 11.628"	N	Y = 4247.42 m. $X = 2474.75 m.$
FFACH LAB	36° 36' 05.571" 121° 52' 33.427"	M	Y = 2009.86 m. $X = 4914.75 m.$

B. ACCURACY ANALYSIS OF HYDROGRAPHIC POSITIONING DATA

The objective of this section is to illustrate how the accuracy of hydrographic positioning data can be classified using Furt's method of circles of equivalent probability. The radius of the 90 percent confidence circle was computed for each position; it provides a quantitative measure of repeatable accuracy.

For subsequent accuracy computations, the following assumptions were made:

- i. The standard error for the microwave ranging system used in the range-range and range-azimuth computations is 3 meters.
- ii. For azimuth-azimuth and range-azimuth positions, the pointing error of the theodolite is 1.3 meters at all ranges.
- iii. The two LOP's involved in all types cf positioning are independent ($\rho_{12}=0$).
 - iv. The data are free of systematic errors.

Raw range and azimuth data were hand logged into a data file for processing. A modification of program UCOMPS was

IV. RESULTS AND DATA ANALYSIS

A. DATA PROCESSING

Automated processing of the positional survey data was done on the NPS IBM 370/3033AP computer system. Graphic displays were constructed using the Display Integrated Software System and Plotting Language (DISSPLA) developed by the Integrated Software Systems Corporation (ISSCO) [Ref. 16]. All computer programs involved in data processing were written in the WATFIV programming language.

computations were made in an X-Y coordinate system based on a Modified Transverse Mercator (MTM) projection. A MTM projection is essentially the same as a Universal Transverse Mercator (UTM) projection, the only difference being that in a MTM projection a central meridian is picked near the survey area instead of being fixed at a particular meridian [Ref. 17].

The central meridian, controlling latitude, and false easting values define the coordinate system used for computations. The central meridian for the projection was chosen to be longitude 1210 52 30 W which is approximately the mean longitude of the survey area. The controlling latitude, the distance ir meters from the equator to a reference latitude, was chosen to be 4,050,000 meters. A false easting of 5,000 meters was chosen as the value of the X-coordinate at the central meridian.

Three shore control stations were used in the acquisition of survey data. The geodetic positions of these stations were converted to the X-Y coordinate system (Table V) using program UCOMPS, which is a hydrographic utility package available to students at NPS.

Trisponder system, a microwave system commonly used for nearshore, line-of-sight survey work. On October 28 and November 30, range-range data were recorded by setting remote units over stations BEACH LAB and MUSSEL. Before and after the survey, the ranging system was calibrated over the fixed base line USE MCN to MUSSEL. Daily checks in the survey area were made to determine if the system was working properly. This was accomplished by maneuvering the survey vessel to a point where two known navigational ranges intersected. One navigational range was formed by stations MONTEFEY AMERICAN CAN COMPANY STACK and MONTEFEY RADIO STATION KMEY MAST. A second navigational range was formed by stations MONTEFEY EARBOR LIGHT 6 and MONTEFEY BLUE LIGHTHOUSE.

Track control for range-azimuth and range-range positions was accomplished by steering the vessel along range arcs. The spacing between range arcs for most lines was planned to be 40 meters. Distance between positions along a sounding line averaged approximately 200 meters. The azimuth-azimuth lines were controlled by steering a magnetic compass heading.

The data acquired under training conditions contained several deficiencies that would normally not be tolerated. For example, the quality of the line steering was generally poor; the vessel wandered off the arc more than 10 meters in several instances. The quality of the sounding lines run using azimuth-azimuth control was extremely deficient; the position plot of these lines show a jagged path by the vessel. Under normal hydrographic procedures, these positions would be rejected. Since the intent of this study is to demonstrate accuracy analysis techniques, these deficiencies prove to be inconsequential; the acquired data are adequate to demonstrate the concepts.

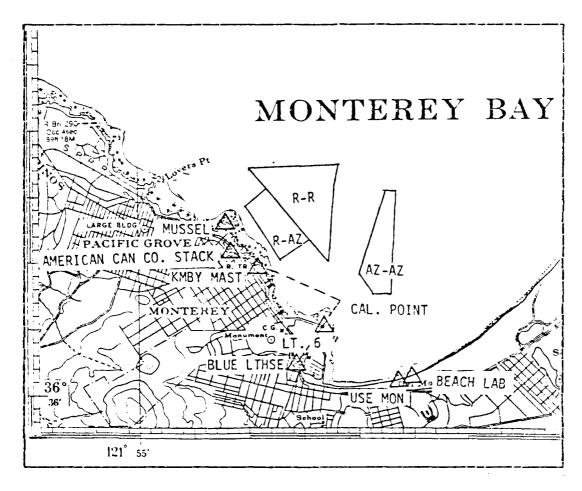


Figure 3.1 Hydrographic Survey Area

all stations are of third-order or better and are published in the National Geodetic Survey Data Base.

For azimuth-azimuth and range-azimuth positioning, azimuths were measured with a Wild T-2 theodolite. On November 16, range-azimuth information was acquired by locating the theodolite over station MUSSEL and initialing on USE MCN. The initial direction was checked by sighting on KMBY MAST. Azimuth-azimuth positions were acquired on November 23. A theodolite was set over USE MON and an initial direction was to MUSSEL. A second theodolite was set at MUSSEL using USE MON for the initial direction.

III. EXPERIMENT DESIGN AND IMPLEMENTATION

The goals of this chapter are to demonstrate that hydrographic positioning accuracy can be classified based or the radii of 90 percent confidence circles determined by using Eurt's method and to show that, based on the same criteria, accuracy predictions can be made for survey planning purposes.

A. DATA ACQUISITION PROCEDURES

The data used for analysis and prediction consisted of range-range, azimuth-azimuth and range-azimuth survey information. The data were acquired by Naval Postgraduate School (NPS) students in a Hydrographic Sciences course. Although the course was structured as a training exercise, the data acquisition procedures utilized were nearly identical to those which are practiced by NOS.

A total of 453 hydrographic positions were recorded during the survey of a nearshore area in southern Monterey Bay, California. Of the positions used for analysis, 292 were range-range, 81 were range-azimuth, and 80 were azimuth-azimuth. All survey information was recorded by hand in sounding volumes. The vessel used was a 36-foot Uniflite with a fiberglass hull and twin engines. The survey was conducted on October 28, November 16, 23, and 30, 1983. Electronic control and calibration stations used for the survey included USE MON 1978, MUSSEL 1932, BEACH LAB 1982, MONTEFEY AMERICAN CAN COMPANY STACK 1932, MONTEREY RADIO STATION KMBY MAST 1962, MONTEREY HARBOR LIGHT 6 1978, and MONTEREY BLUE LIGHTHOUSE (Fig. 3.1). With the exception of MONTEREY BLUE LIGHTHOUSE, which is a low-order position,

Given the frequency of 1.6 MHz, λ = 187.37 meters from Equation 2.3. The lare width along the base line is w'= 93.68 meters from Equation 2.5. Using the law of cosines from plane geometry, the subtended angles α_{a} and α_{a} are 32.47° and 43.25°, respectively. The angle of intersection of the two hyperbolas at P is 37.860 from Equation 2.7. lane widths at P are $w_r = 254.19$ meters and $w_g = 335.06$ meters from Equation 2.6. The standard errors of the green (σ ,) and red (σ ,) hyperbolas, respectively are σ , 16.7 meters and $\sigma = w \sigma = 12.7$ meters. These standard errors are in a linear skewed coordinate system and must be transformed to an uncorrelated rectangular system. From Equations 2.18 and 2.19, the values of $\sigma_{\rm p}$ and $\sigma_{\rm h}$ are 36.9 meters and 12.7 meters, respectively. The correlation coefficient in the correlated rectangular system (o_{ab}) is then 0.737 frcm Equation 2.26. The semi-major and semi-minor axes in the uncorrelated rectangular system are 38.1 meters and 8.3 meters, respectively, from Equations 2.27 and 2.28. The eccentricity is

$$c = \frac{\sigma_{y}}{\sigma_{x}} = 0.218$$

Table IV is entered with the values of P = 0.9 and c = 0.218. The value for K is found to be

$$K = 1.6602$$

From Equation 2.37, the radius of the 90 percent probability circle is found to be

R = 63.3 meters

The probability that the vessel's position will be within a circle of 63.3-meter radius centered at the intersection of the LCP's is 90 percert.

$$\sigma = \sigma = 1.3 \text{ meters}$$

then

$$c = \frac{\sigma_{\mathbf{Y}}}{\sigma_{\mathbf{x}}} = 0.433$$

Table IV is entered with the values of P = 0.9 and c = 0.433. The value for K is found to be

$$K = 1.7117$$

Using Equation 2.37, the radius of the 90 percent probability circle is found to be

$$R = 5.14$$
 meters

The probability that the vessel's position will be within a circle of 5.14-meter radius centered at the intersection of the ICP's is 90 percent.

Example 3

A vessel is conducting a hydrographic survey using hyperbolic-hyperbolic geometry. The hyperbolic LC? generated by the 1.6-MHz electronic positioning system has a standard error of 0.05-lane on the base line. The correlation coefficient (o) between the two LOP's is known to be 0.4. Compute the radius of the 90 percent confidence circle at the vessel's position.

The rectangular plane coordinates of the master (M), two slaves (G and P), and the vessel's position (P) are

	X COOPDINATE	Y COCRDINATE
	(m)	(m)
Ď.	172,679.1	62,540.4
G	308,679.1	98,540.4
M	241,738.2	21,325.4
P	223,172.5	169,264.2

Example 1

A vessel is conducting a hydrographic survey using range-range geometry. The two LOP's generated by microwave transmitters have standard errors of $\sigma=3$ meters and $\sigma=4$ meters. The angle of intersection 8 at the vessel is 30°. Assume the LOP's are uncorrelated. Compute the probability that the vessel's position will be within a circle of 10-meter radius with the center at the intersection of the LOP's.

Recalling Equations 2.18 and 2.19, the values of σ_{x} and σ_{y} are found to be 9.79 meters and 6.14 meters, respectively. From Equation 2.36

$$c = \frac{\sigma_{\mathbf{y}}}{\sigma_{\mathbf{x}}} = 0.633$$

and from Equation 2.37, with R = 10 meters,

$$K = 1.032$$

Entering Table III and using interpolated values for c and K, the probability that the vessel's position will be within a circle of 10-meter radius centered at the intersection of the ICP's is

$$P = 53.2\%$$

Example 2

A vessel is conducting a hydrographic survey using range-azimuth geometry. The range LOP generated by the microwave transmitter has a standard error of 3 meters. The azimuth LOP determined by theodolite observation has a standard error of 1.3 meters at all ranges. Compute the radius of the 90 percent confidence circle at the vessel's position.

In the range-azimuth case β = 90° and the ICP's are uncorrelated. Therefore,

$$\sigma_1 = \sigma_x = 3.0 \text{ meters}$$

and

confidence ellipse is

$$A_e = K_\sigma^2 x^\sigma y^\pi \tag{2.38}$$

where K is the appropriate probability conversion factor (Table I). The area of the 90 percent confidence circle is

$$A_{C} = \pi R^{2} \tag{2.39}$$

where R is given by Equation 2.37. For a condition where $\sigma_1 = \sigma_2 = 3$ meters, and $\beta = 30^\circ$, the area of the 90 percent confidence ellipse is 261 square meters, while the area of the confidence circle is 587 square meters. For both standard errors equaling 10 meters and $\beta = 30^\circ$, the 90 percent confidence ellipse has an area of 921 square meters and the confidence circle has an area of 2894 square meters. From an operational perspective, the difference in areas between ellipses and circles have significant implications which will be discussed in Chapter V.

The following examples are presented to demonstrate methods for computing the parameters of error ellipses and confidence circles for several hydrographic positioning geometries.

TABLE III Probabilities, Given c and R

\	0.0	0.1	0. 2	0.3	0. 4	0.5	0.6	0.7	0. 8	0.9	1 0
0. 1 0. 2 0. 3 0. 4 0. 5	0796557 1585194 2358228 3108435 3829249	0443987 .1339783 .2213804 .3010228 .3755884	0242119 0884533 1739300 . 2635181 . 3481790	. 0154176 . 0628396 . 1318281 . 2139084 . 3003001	0123875 - 0482413 - 1039193 - 1742045 - 2532953	. 0099377 . 0390193 . 0851535 . 1451808 . 2152886	0092940 0327123 0719102 1237982 1557448	0071157 0281415 0621386 1076237 1620829	. 0062299 . 0246824 . 0546598 . 0956495 . 1443941	. 0053400 0219757 0487639 0850326 1296286	00496 014 04400 071-95 11730
0. 6 0. 7 0. 8 0. 9 1. 0	4514938 5160727 5762892 6318797 6826895	4457708 5115046 5725957 6288721 6802325	. 4255605 4960683 . 5604457 6191354 6723588	. 3846374 . 4633258 . 5349387 . 5993140 . 6568242	. 3357384 . 4170862 4941882 . 5651564 . 6291249	. 2914682 . 3699305 . 4474207 5213598 . 5900953	. 2548177 3280302 4025628 4759375 5461319	. 2251114 2925654 . 3627122 . 4333628 . 5025790	2009797 2020373 3253453 3953279 4621421	1811753 2351553 2959760 3720135 4257553	16472 21724 273×5 33302 39346
1. 1 1. 2 1. 3 1. 4	7286679 7698607 8063990 8354867 8663856	7266597 7682215 8050648 8374049 8655127	7202682 7630305 8008554 8340018 8627728	. 7079681 . 7532175 . 7929968 . 5277046 . 8577362	. 6859367 - 7359558 - 7793550 - 8169851 - 8493071	. 6524489 . 7079973 . 7567265 . 7989288 . 8350816	6116316 6714269 7249673 7720589 8129287	. 5687467 6306168 6873122 7353089 . 7833962	5272462 5893494 6474394 7007900 7489500	4857873 5495736 6070822 6023035 7122546	41399 51324 57044 62169 67534
1 6 1.7 1 8 1.9 2.0	. 8904014 . 9108691 . 9281394 . 9425669 . 9544997	8897008 9103102 9276964 9422182 9542272	3875060 9085619 9263125 9411299 9533775	\$834914 9053768 9237989 9391586 9518415	8768644 9001746 9197275 9359855 9493815	. 8657559 . 8915536 . 9130680 . 9308615 . 9454546	8478393 8773116 9019110 9222277 9358418	.8226246 9562471 9846624 9093609 .9278799	7917194 9291137 8613238 9896731 9115762	7574708 7977852 8332175 8639149 8901495	7219/ 74/25 90210 - 83/52 9640/
2 1 2 2 2 3 2 4 2 5	9642712 9721931 9785518 9536049 9875807	. 9640598 . 9720304 . 9784275 . 9835108 . 9875100	9634011 9715237 9780408 9832180 9872900	. 9622127 . 9706109 . 9773450 . 9626918 . 9568953	9603170 9691597 9762419 9818594 9862720	. 9573205 . 9668845 . 9745239 . 9805703 . 9853112	9522999 9631017 9716934 9784661 9837369	9437668 9565522 3667306 9747495 9810035	9305013 9459386 9583739 9582698 9769522	9122714 9306821 9458095 9580804 9673136	91107 91107 9259 94350 95606
2. 8 2. 3 2. 9 3. 0	9906776 9930661 9948597 9962684 9973002	9906249 9930271 9943612 9962477 9972853	9904612 9929062 9947727 9961834 9972391	9901674 9926894 9946141 9960684 9971564	2897045 9923483 9943649 9958878 9970266	. 9889934 . 9918260 . 9939842 . 9956126 . 9968294	9878527 9909944 9935821 9971798 9965205	9858331 9595268 9923249 9944246 9959854	9821023 9867530 9902888 9929452 9949274	9517837 9517837 9564976 9900803 9927923	96591 97041 9401 94101 94101
3. 1 3. 2 3. 3 3. 4 3. 5	. 9980648 . 9986257 9990332 . 9993261 . 9995347	9980542 9986182 9990279 9993225 9995323	. 9980212 . 9985949 . 9990116 . 9993112 . 9995245	9979622 9985533 9989824 9992909 9995105	9978699 9984880 9989368 9992593 9994888	. 9977296 . 9983592 . 9985677 . 9992115 . 9994539	. 9975109 . 9982356 . 9987607 . 9991376 . 9994053	9971348 9979733 9955792 9990129 9993204	9963851 9974478 9992147 9957626 9991502	9948168 , 9963105 9974004 , 9981868 9957480	. 99181 . 99402 . 9956 99631 99781
3. 6 3. 7 3. 8 3. 9 4. 0	9996818 9997944 9998553 9999038 9999367	. 9996801 . 9997832 . 9998545 . 9999033 . 9999363	9996748 9997797 9995522 9999018 9999353	9996653 - 9997733 - 9998478 - 99989 9999334	. 9996505 . 9997633 . 9998412 . 9998945 . 9999303	9996281 9997452 9998311 9998578 9999261	9995938 9997251 9998157 9998776 9999195	. 9995364 . 9996567 . 9997902 . 9995606 . 9999085	9974218 9996102 9997396 9945276 9998870	. 9941442 . 9994208 . 9996119 . 9997426 . 9998309	. 99546 . 9959 . 99926 . 94950
4 1 1 4 2 1 4 3 4 4 4 5	. 9999587 . 9999733 . 9999829 . 9999892 . 9999932	. 9999585 ; . 9999732 ; . 9999828 ; . 9999891 ;	. 9999518 . 9999727 . 9999826 . 9999889 . 9999931	. 9299566 . 9999720 . 9999821 . 9399886 . 9999929	. 9999547 . 9999707 . 9999813 . 9999881 . 9999925	. 9999519 . 9999689 . 9999801 . 9999874 . 9999921	9999475 9999661 9999753 9999863 9999914	9999404 9999616 9999754 9999845 9999902	. 9999266 . 9999527 . 9999698 . 9999409 . 9999881	. 9998900 . 9999292 . 9999548 . 9999715 . 9999822	99977 999*5 99990 99993 90995
4 A 4 7 4 8 4 9 5 0	9999958 9999974 9999984 9999999	9999957 9999974 9999984 9999990 9999994	9999957 9999973 9999984 9999990	9999955 9999973 9999983 9999990 9999994	. 9999954 . 9999971 . 9999983 . 9999990 . 9999994	. 9909951 . 9999970 . 9999982 . 9999989	9999947 9999957 9999950 9999958 9999993	. 9992939 9499963 9999977 . 9994986 9999992	9991926 9999955 9999972 999993 9999990	9999589 9999432 9999959 9999375 9994955	99997 99999 99999 99999
5. 2 5. 3 7. 4 5. 5	. 9999997 . 9999998 . 9999999 . 9999999 . 0000000	9999997 9999999 9999999 9999999 1.0000000	. 9999997 9999998 9999999 9999999 0000000	. 9399996 9329998 . 9399999 9349339 1. 000000	9999996 9999999 9999999 1.000000	. 9999996 . 9999998 . 9999999 . 9999999	9990996 . 0999998 . 9990999 . 9990999 1. 0000000	9999995 9999997 9999998 9999999 9999999	. 9999994 . 9999997 . 9999998 . 9999999	4999991 999995 999999 9999999	99969 94969 94999 99999
5. 6 5. 7 5. 9 5. 9	; ;	; 						1. 0000000	1. 9000000	. 9999999 1. 0000000	99999 99999 1-00000

b. Circles of Equivalent Probability

Burt [Ref. 3] presents a method for translating ellipses of equivalent probability into circles of equivalent probability. To utilize this method, it is first necessary to compute the eccentricity of the error ellipse, c, by the equation

$$c = \frac{\sigma_y}{\sigma_x} \tag{2.36}$$

where $\sigma_{\mathbf{x}} > \sigma_{\mathbf{y}}$.

Harter [Ref. 15] compiled Tables III and IV which are taken from Bowditch [Ref. 10, p. 1215]. Harter's data are given in terms of the eccentricity, c, a parameter, K, and a probability, P. The parameter, K, when multiplied by $\sigma_{\mathbf{x}}$ gives the value of the radius, R, of the circle of the corresponding probability shown in Table III. That is,

$$R = K \sigma_{\mathbf{x}} \tag{2.37}$$

The probability of a point falling inside a circle of specified radius can be computed by entering Table III with c and K as arguments. Given a fixed probability, K is determined by entering Table IV using c and P as arguments. The radius of the probability circle is then computed using Equation 2.37.

Using confidence ellipses has certain advantages over confidence circles of equal probability. First, the directional nature of the true error distribution is not represented in the confidence circle method even though both methods give an accurate measure of confidence. Second, the area of the confidence ellipse is always less than or equal to the area of the confidence circle. The area of a

- i. 0.5 mm at the scale of the survey for scales of 1:20,000 and smaller,
- ii. 1.0 mm at the scale of the survey for 1:10,000 scale surveys, or
- iii. 1.5 mm at the scale of the survey for scales of 1:5,000 and larger.

The major advantage of using d_{rms} as a precision index is its ease of computation. Some hydrographers draw analogy between the varying probability associated with one d_{rms} (63.2 percent to 68.3 percent) and the fixed probability associated with a one-dimensional standard error (68.3 percent). In fact, d_{rms} has very little statistical meaning. The obvious problem with using d_{rms} as a precision index is the varying probability associated with the error circle. For this reason Greenwalt [Ref. 12, p. 31] recommends against its use.

Р	T robabilities	ABLE II Associate		ms
y 0100000000000000000000000000000000000	1.0 1.1 1.1 1.1	TH OF drms 0000 0020 020 042 077 118 166 2280 345	PROBABII 1 drms 0.683 0.682 0.682 0.676 0.671 0.662 0.650 0.641 0.635 0.632 0.632	2 d rms 0.954 0.955 0.961 0.966 0.969 0.973 0.977 0.980 0.981

An error circle with a radius of one d rms constructed about the intersecting LOP's (Fig. 2.9). Two d is the radius of the error circle obtained using two rms times the values of $\sigma_{\mathbf{x}}$ and $\sigma_{\mathbf{y}}$ in Equation 2.31. For an elliptical error distribution, the probability associated with a specific value of d varies as a function of the eccentricity of the error ellipse (Table II). The probability associated with one d varies from 63.2 percent to 68.3 percent, while the probability associated with two d rms varies between 95.4 percent and 98.2 percent.

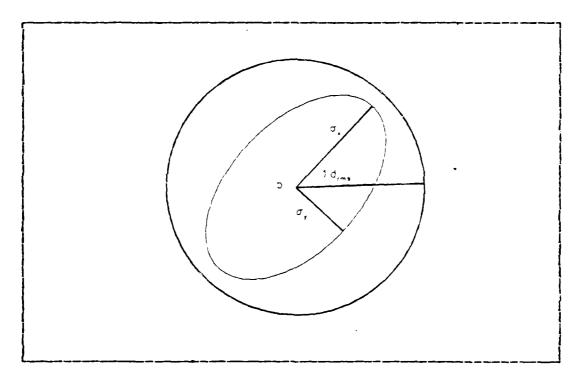


Figure 2.9 The d_{rms} Error Circle

NOS uses d_{rms} as an accuracy specification. Umbach [Ref. 14, p. 4-25] states that super high frequency direct distance measuring systems would be used only when the value of d_{rms} is less than or equal to:

distribution can be substituted for the elliptical distribution. This substitution can be satisfactory for error analysis within certain ${}^\sigma y'{}^\sigma x$ ratios. However, when this ratio is small the distortion introduced by the circular distribution may become misleading.

a. Root Mean Square Error

The terms radial error, root mean square error, and d_{rms} are identical in meaning when applied to two-dimensional errors [Ref. 10, p. 1229]. The term d_{rms} is defined as the square root of the sum of the squares of the standard errors along the major and minor axes of the error ellipse. That is

$$d_{rms} = \sqrt{\sigma_x^2 + \sigma_y^2}$$
 (2.31)

where $\sigma_{\mathbf{x}}$ and $\sigma_{\mathbf{y}}$ are given by Equations 2.18 and 2.19. A more direct form of 2.31 is given by [Ref. 2, p. 54]

$$d_{rms} = \frac{1}{\sin \beta} \sqrt{\sigma_1^2 + \sigma_2^2}$$
 (2.32)

for uncorrelated LOP's. For range-range and azimuth-azimuth positioning, with $\sigma_1 = \sigma_2 = \sigma$, Equation 2.32 reduces to

$$d_{rms} = \frac{\sqrt{2}}{\sin \beta} \sigma \qquad (2.33)$$

For range-azimuth positioning, $\beta = 90^{\circ}$ and Equation 2.32 becomes

$$d_{rms} = \sqrt{\sigma_1^2 + \sigma_2^2}$$
 (2.34)

The mcre general form of Equation 2.32 for both correlated and uncorrelated LOP's [Ref. 2, p. 59] is

$$d_{rms} = \frac{1}{\sin \beta} \sqrt{\sigma_1^2 + \sigma_2^2 + 2\rho_1 \sigma_1 \sigma_2 \cos \beta}$$
 (2.35)

where ρ_{12} is the correlation coefficient.

used to compute X-Y coordinates of all positions. Based on geometric relationships discussed earlier, angles of intersection of the LCP's were then computed for range-range and azimuth-azimuth points. The angles of intersection for all range-azimuth positions are 90°.

The range-range and azimuth-azimuth data were then passed to WATFIV subroutine PRCB (Appendix A). As input parameters, the subroutine accepts two standard errors of the LCP's and the corresponding angle of intersection. The output parameters include the semi-major and semi-minor axes of the 90 percent confidence ellipse, the radius of the 90 percent confidence circle, and the areas covered by both figures.

Subroutine PROB uses a linear approximation to determine the value of the function K for varying values of the eccentricity, c, in Burt's method. A linear interpolation was performed by first taking the eleven discrete values of c and K for a probability of 90 percent from Table IV and then constructing a series of relationships for K as a function of c (Table VI).

Values of the radii of 90 percent confidence circles for range-range data were plotted at their respective positions (Fig. 4.1). The arcs of circles connecting the two control stations BEACH LAB and MUSSEL represent lines of constant intersection angle (30°). Of the range-range data set, position 848 (Appendix B)—coordinates X = 4119.01, Y = 4735.C7—was found to have the smallest radius (strongest position) of 6.4 meters and an angle of intersection of 90.2°. Position 137—coordinates X = 3345.86, Y = 3873.34—represents the weakest position with radius value of 15.3 meters and an angle of intersection of 26.7°.

The positional accuracy degrades rapidly as the intersection angle approaches 30°; the 30° arc represents a line of constant 13.7 meter radius. Within 400 meters of the 30°

<u>Interval of c</u>	<u>Linear Interpolation</u> <u>Function For K</u>
0.0 - 0.1 0.1 - 0.2 0.2 - 0.3 0.3 - 0.4 0.4 - 0.5 0.5 - 0.7 0.7 - 0.8 0.8 - 0.9 0.9 - 1.0	K = .0306c + 1.64485 K = .0940c + 1.63851 K = .1652c + 1.62427 K = .2535c + 1.59778 K = .3790c + 1.54758 K = .5444c + 1.46488 K = .7101c + 1.36546 K = .8508c + 1.26697 K = .9475c + 1.18961 K = 1.0361c + 1.10987

intersection arc, the radius varies between 8 and 15 meters. The radii values charge slowly in the vicinity of the minimum value of 6.4 meters which corresponds to an angle of intersection of 90°.

The radii of 90 percent confidence circles associated with the azimuth-azimuth positions acquired using control stations USE MON and MUSSEL were also plotted at their respective positions (Fig. 4.2). The standard errors of the LOP's are assumed to be 1.3 meters; the resulting improved accuracy is evident. The maximum value of the 90 percent confidence circle radii is 8.7 meters at position 637--coordinates X = 4327.25, Y = 2818.39--which corresponds to an angle of intersection of 159.80 (or in terms of the supplement, 20.20). Fosition 682--coordinates X = 4611.20, Y = 4421.29--represents the strongest position recorded during the survey with a 90 percent confidence circle radius of 2.8 meters and an angle of intersection of 91.00.

Again, the rapid degradation of accuracy is noted approaching β = 150°. The arc of the 150° intersection angle represents a constant radius of 5.9 meters. Discrete

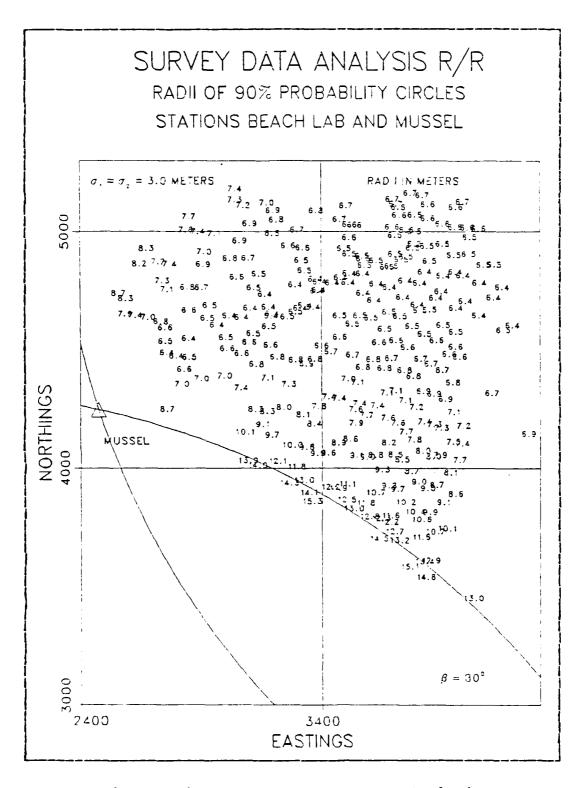


Figure 4.1 Range-Range Accuracy Analysis

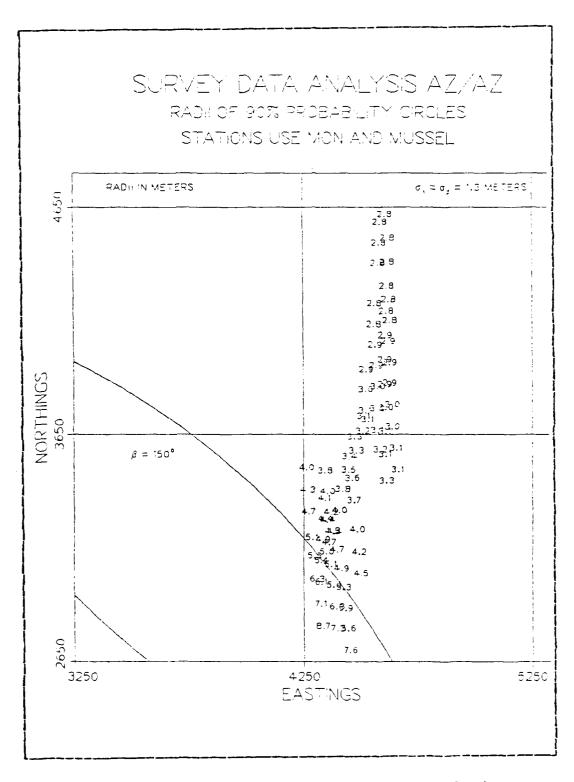


Figure 4.2 Azimuth-Azimuth Accuracy Analysis

values along the arc confirm this qualitatively. A large area of strong positional accuracy surrounds the area where β = 90°. Numerous values of 2.8 meters are present near the top of the plot.

Using the assumptions stated at the beginning of this section, the values for all radii of 90 percent confidence circles for range-azimuth positions are 5.1 meters. This computation was carried out in Example 2 of Chapter II. Since this case is trivial, the data are not displayed graphically.

Positioning data were also classified based on the parameters of the 90 percent confidence ellipse. WATFIV program FILIP (Appendix C) was used to generate the parameters of the 90 percent confidence ellipse for range-range, azimuth-azimuth, and range-azimuth positioning data. The program was initialized by entering the coordinates of the control stations and standard errors of the LOP's. The fix number, hydrographic position coordinates, and angle of intersection were then read in from a data file. Subroutine PROB was called to compute values for $K\sigma_{\mathbf{x}}$ and $K\sigma_{\mathbf{y}}$.

The angle of orientation of the major axis of the ellipse, measured clockwise from north, was then computed. For range-range and azimuth-azimuth positions, the LCF generated from the left control station was used as the base LOP. For range-azimuth positions, the LOP formed by the theodolite was used as the base LOP. First, the orientation of the base LOP in the coordinate system was determined. The orientation of the major axis of the error ellipse relative to the base LOP (0) was then computed using Equation 2.29. By adding or subtracting 0 to the orientation of the tase LOP, the orientation of the major axis of the error ellipse in the coordinate system was determined. This angle takes on values from 00 to 1800. Appendix D consists of the confidence ellipse classification scheme for range-range,

azimuth-azimuth and range-azimuth data. Forty positions for each positioning geometry are listed for comparison to the classification scheme presented in Appendix 3.

Appendix B lists the data by position number, X-Y ccordinate, angle of intersection, and radius of the 90 percent confidence circle. Appendix D lists the data by position number, X-Y coordinate, angle of intersection, K_{σ} , K_{σ} , and angle of orientation for the 90 percent confidence ellipse. These appendices are similar to hydrographic survey data bases and demonstrate accuracy classification schemes based on the two criteria.

C. ACCURACY PREDICTIONS

The cverall positional accuracy of a survey can be controlled by computing accuracy values before data acquisition is begun. For example, if the hydrographer is using radii of 90 percent confidence circles as an accuracy criterion, the minimum allowable angle of intersection for two ICP's can be computed for meeting specifications. The nature of the survey area may allow the flexibility to change system geometry to maximize accuracy at a specific location or to maximize the area covered with a given accuracy. By making accuracy computations before acquiring data, the hydrographer may also have the option of deciding what type of positioning system is to be used to meet accuracy requirements.

The construction of reliability contours is one method to display the expected positional accuracy. Reliability contours, lines of constant repeatable accuracy which are functions of the system geometry and standard errors of the positioning equipment, can be constructed about shore stations using the radii of 90 percent confidence circles criterion or the less desirable d_{rms} value.

Consider the equations that have been developed in Chapter II for the determination of radii of 90 percent confidence circles using Burt's method. For uncorrelated IOP's in a range-range or azimuth-azimuth system, the repeatable accuracy of a hydrographic position is a function only of the angle of intersection, assuming the standard errors of the LOP's are constant throughout the survey area. The locus of points which define a constant angle of intersection for two LOP's in a range-range or azimuth-azimuth system is a circle which passes through both control stations. Given the coordinates of the two control stations, the equations of these circles can be determined.

Construction of reliability contours involves several simple trigonometric relationships (Fig. 4.3). Let IR he the line connecting the two shore control stations L and R in a range-range system. The length of line LR is h. The circle through both stations defines a line of constant intersection angle for two LOP's. The radius of the circle is r. The distance e is measured along the perpendicular hisector of the line IR to the center of the circle at point O(h,k) and is given by

$$e = \frac{b}{2\tan\beta} \tag{4.1}$$

Knowing e and the radius r, the coordinates of point 0 can be computed. The equation of the circle is then

$$r^2 = (x - h)^2 + (y - k)^2$$
 (4-2)

These two equations were used to generate reliability contours for display on a computer graphics terminal. Using Eurt's method, the angles of intersection of two LOF's were computed for discrete values of radii of 90 percent confidence circles. Reliability contours about stations EFACH

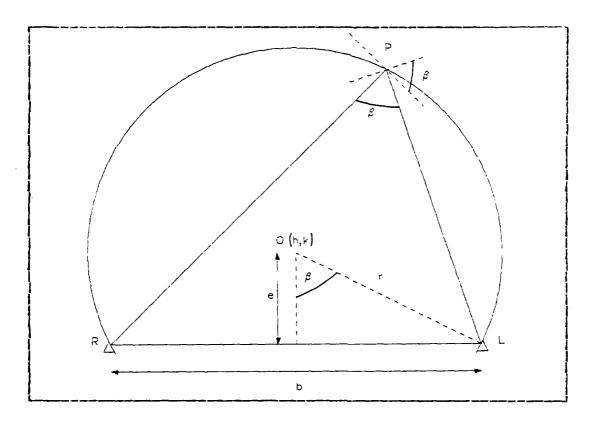


Figure 4.3 Construction of a Reliability Curve

LAB and MUSSEL for a range-range system ($\sigma_1 = \sigma_2 = 3$ meters) were constructed (Fig. 4.4). Using Equation 4.2, X-Y coordinates were generated for points laying on different reliability circles. A curve-fitting subroutine in the DISSPIA library was used to generate the circles through the computed points. The 13-meter accuracy contour corresponds to an angle of intersection of 31.6°, while the 7-meter accuracy contour corresponds to an angle of intersection of 67.9°. The best achievable accuracy of the system is 6.4 meters at 90°.

For comparison purposes, reliability contours were constructed about BEACH LAB and MUSSEL for azimuth-azimuth geometry ($\sigma_1 = \sigma_2 = 1.3$ meters). The increased accuracy of this configuration is evident (Fig. 4.5). The 3-meter

contour corresponds to an angle of intersection of 69.4° while the 6-meter contour corresponds to an angle of intersection of 29.6°. The best achievable accuracy at an intersection angle of 90° is 2.8 meters.

A second scheme was used to display accuracy predictions for the two positioning methods. Given the coordinates of PEACH LAB and MUSSEL, a series of discrete points spaced 800 meters apart, were generated throughout the survey area. The values for the radii of 90 percent confidence circles were then computed at each point with the use of subroutine FROB. Figures 4.6 and 4.7 illustrate this prediction scheme. These figures present the same information as Figures 4.4 and 4.5 in a different manner. The 30° angle of intersection contour is shown on both figures.

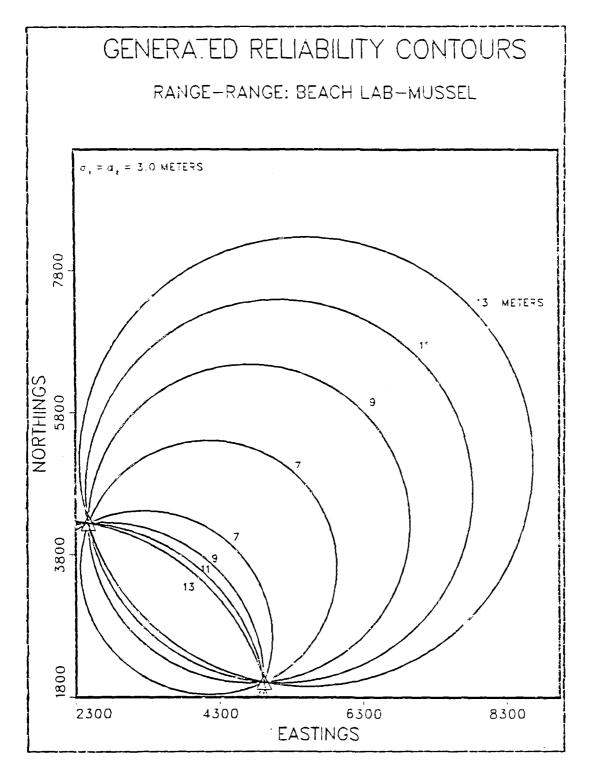


Figure 4.4 Reliability Contours: Range-Range Geometry

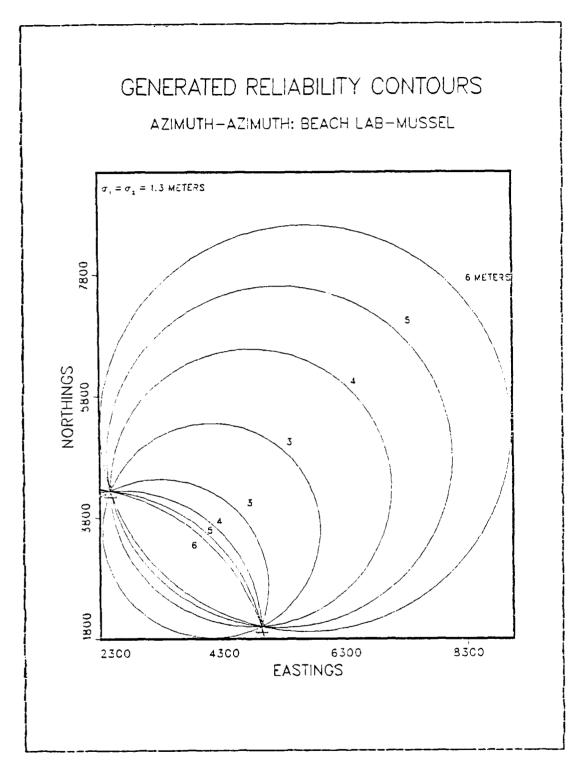


Figure 4.5 Reliability Contours: Azimuth-Azimuth Geometry

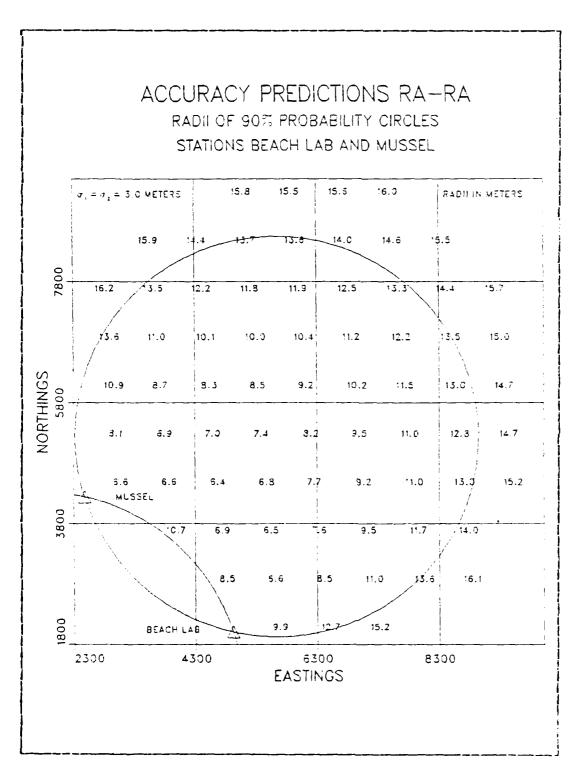


Figure 4.6 Range-Range Point Accuracy Prediction

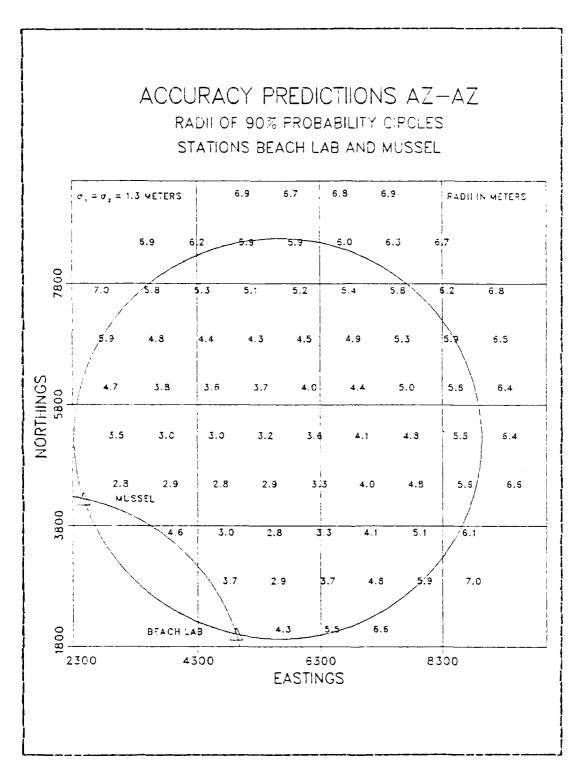


Figure 4.7 Azimuth-Azimuth Point Accuracy Prediction

V. CONCIUSIONS AND RECOMMENDATIONS

A. ACCURACY SPECIFICATIONS

Interpretation of the 1982 IHO positioning standards in terms of 90 percent confidence circles yields some interesting results with respect to present day survey practices. For example, for a 1:10,000-scale hydrographic survey, NOS usually uses microwave positioning systems in a range-range mode, and assumes a standard error of 3 meters for each LCP. Surveys are frequently conducted between the 30° to 150° angle of intersection limits. Using the 90 percent confidence circle criterion, the radius of the circle should not exceed 10 meters. However, the radius value for $\beta = 30°$ and 150° is 13.7 meters. The values of Ko_x and Ko_y for the 90 percent confidence ellipse are 17.6 and 4.7 meters, respectively. To meet the 90 percent criterion for a 1:10,000-scale survey, the β limits should be 42° to 138°.

Azimuth-azimuth positioning is accurate enough for 1:5,000-scale surveys, using 8 limits of 35° to 145°, assuming a standard error of 1.3 meters for each LCP. With the standard error assumptions used for range-azimuth, the 90 percent radius is 5.1 meters for all positions. Given the uncertainties of the standard error figures, it is rational to assume that range-azimuth positions can meet the 5-meter accuracy standard for 1:5,000-scale surveys. In fact, range-azimuth positional accuracy can exceed azimuth-azimuth accuracy when the later's 8 is less than 35°. For a 3-meter 5 range-range configuration, it is impossible to meet 1:5,000 specifications with any 8.

As a general guideline, the 30° to 150° angle of intersection limit is a good rule to use for uncorrelated LCF's.

CLASSIFIED AZIMUTH-AZIMUTH POSITIONS
Control Stations: USE MON 1978 and MUSSEL 1932
Standard Error Used in Computations: 1.3 meters

Fix No.	<u>Coordinate</u>			Radius of 90% circle
\$0123456781234567890123456789011234567890112345678901234578901 1222222222333333333344444444445555555555	2846465373997514275205996752353743973800962046245083019100359 977990064848377223474677556043305081802420477230579344762233 4321197648337722347467755604330508180242047723057798430361762433 43241976433333322222987654560433050818024204772305779843036176243333333333333333333333333334345555555444607763443036176243	097604424158239096936682512608976310633506499959727780642233717792449121097266380620806083750742252157687989220776106290311779244912109726863807566188745671770899875311008990111009988716202243220976644447675665431098776657431099877765789012345321012345567890123456756678901245565	906243925717890380041956418781122954019222458709698026703519 639631863058261596285183714714940517417963963956418630729657 1514143333334455555544443333444554333221111111111	659m97+2081484117m7617+0m715m15085m2109520754m12100998888888887655444455565444mmmmmmnmmmmmmmnnn222222

RANGE-RANGE ACCURACIES (CONTINUED)

Fix No.	X <u>Ccordinate</u>	Y <u>Coordinate</u>	Angle of <u>Intersection</u>	Radius of 90% circle
6769011334567890113345678901133456789011334567890113345678901133456789011334567890113345678901133456	47179912418260333025286481022658685135372179881072 576717839796131713878208934176329207845727003685654 377286618111113878208934176329207845727003685654 58703486181111138616617114116927245248611997111261156 588999999988877889999999999999999999999	388567998470198231190151736566891663967439749345845 31997877800670523846956324084138716332419088091047 34869615594914910583858317357714098567939775208964497 431975296641318869819405559258766423199375789110876 876432198876108754111097568901098768901109757891110876	834180919965776725292561434876367808283415200303427 283827046804949281570177272517386260530625059340526 98877666543319998876655542899100998899100998999900998	4456805111747554664277778044566666666666666666666666666666666666

RANGE-RANGE ACCURACIES (CONTINUED)

$\underbrace{\mathtt{No}}_{\bullet}$	X	Y	Angle of	Radius cf
	<u>Coordinate</u>	<u>Coordinat∈</u>	Intersection	90% Circle
77777777777777777777777777777777777777	09004113407388829220537866533222538301383569009497256763000696860 57912120007744360264813795597765442374156648334951641116464611869 0.0.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1	0640947592862192781654163259353034472496821406657464539510835969 524239152085678918542306155563447027912319841065991845981333319698 6328151915250807432918653241058329188653281333319698 320740730112566027472918655324105813713864688518282674689695 87643209878901345678876542108777890234688652992244684689094 444444433333344444444444444333333444444	8094154073740352665817955814162204386189016010537416765585297540 2704791338531852840559371479121085285273616159257975296284050597 98876554323455677899988776544334456678899988766543234456678899999	#45700583567571865455456828727270987666666667789051987766666666666667789241987766666666666666666666666666666666666

RANGE-RANGE ACCURACIES (CONTINUED)

Fix No.		Y <u>Coordinate</u>	Angle of <u>Intersection</u>	Radius of 90% Circle
11111111111111111111111111111111111111	714676282769968036331604935454719824459528158078587842580097988605925764650962373874293687339960076009686237756434398794267813421259667621921266676768621666164459323755646982373599662478559667698527556666666666666666666666666666666666	76303163724242172480264430834450573409999868979481709111486088 17690089877078025378828028620889666610930112515997800943249506519 1837100120443456037400469038707617278842803177136883996907152655946 136664209992466420980357653199913366057806884678642088900122345678 4444433344444333444444334444444444444	0785993687743276070304745208644758904758966717767410111168076272 2337135811056272964167681844078023371596217811123329529639617383 46887532357887542246788764335679987665543345789987643333455677889	0354817304955889136464474929506445714961500785445748887326186544 1118666679459766667821876666677777923976666666781209877666666

RANGE-RANGE ACCURACIES (CONTINUED)

Fix	<u>Coordinate</u>	<u>Ccordinate</u>	Angle of Intersection	Radius of 90% Circle
1\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	05.61141232325692421554980635352638614023636732048815210390979025287381138447331870782891503152541876594976650394206189177276264841330095238048497848880297414447264555102632902558772122887122995412596629967792102880135707511864497630742063290255807721228871129995412963291346531988013570751390905511864497630742063290210011111111110222	8326859505419753902897889893672679964098020778872481444410773042 5657329066542335570343104265942191694471104274199328102258630802255 6727907220256189731215986130981223426534891714026629839546341413 74081546789098654356763998461309881223426534891714026629839546341413 746546789098654356789087653209764542199764913556803110246410135556420 44444444444444444444444444444444444	5856660483475970954740391551234430735006339957386585741389863323 641603689639467060470516089073921823774218039532119261177935271354 9998999991	55444445565445605445566445678666666666678912237666666678911111

APPENDIX B ACCURACY CLASSIFICATION: 90 PERCENT CONFIDENCE CIRCLES

CLASSIFIED RANGE-RANGE POSITIONS

Control Stations: BEACH LAB 1982 and MUSSEL 1932

Standard Error Used in Computations: 3 meters

Fix	X	Y	Angle of	Radius of
No.	<u>Ccordinate</u>	<u>Ccordinate</u>	Intersection	90% <u>Circle</u>
127456789012745678901274567890127890123456890 111111111112222222222222233333333333344444444	5187666061333215744751866458983727278376983448338 00522041066133040249419333643988740074009073911938 8210849528711440373722446673097913727924468 6524877557901679023108678025642087779131377753 22332222233222222233322223333333333	79545367373529131765043068511777526977802016565235 0687373463260836574062709373379793053883425551615 2648172534666955873995541708126193153108014437391 9779427581230726024769955417081226193153108014437391 9011087801108768920167789010975379125652880503441889 4555554444555554444445555444445555444444	06602943607499078298253918178924003077771544069635 7187.0	274362773201429309941998&888888876777666666666666666666666666

```
ELSE IF ((C.1E.0.6).AND. (C.GT.0.5)) THEN

ELSE IF ((C.1E.0.6).AND. (C.GT.0.4)) THEN

ELSE IF ((C.1E.0.5).AND. (C.GT.0.4)) THEN

ELSE IF ((C.1E.0.4).AND. (C.GT.0.3)) THEN

B=0.2535*C+ 1.59778

ELSE IF ((C.1E.0.3).AND. (C.GT.0.2)) THEN

ELSE IF ((C.1E.0.3).AND. (C.GT.0.2)) THEN

ELSE IF ((C.1E.0.2).AND. (C.GT.0.1)) THEN

ELSE IF ((C.1E.0.2).AND. (C.GT.0.1)) THEN

ELSE B=0.0306*C+1.64485

END IF

RADIUS=B*SICX

SGX90=2.146*SIGX

SGY90=2.146*SIGY

CIRAR=3.1415926*RADIUS**2

ELAR=3.1415926*SGX90*SGY90

FETURN

END
```

APPENDIX A

SUERCUTINE FOR 90 FERCENT CONFIDENCE CIRCLE PARAMETERS

```
SUERCUTINE PROE (SIG1, SIG2, COR, TBETA, SGX90, SGY90, * RADIUS, ELAR, CIFAR) INFLICIT REAL*4 (A-H, O-Z) COMPUTES RADIUS OF 90% CONFIDENCE CIRCLE (BURT, METHOD THIS SUBROUTINE WORKS FOR CORRELATED AND UNCORRELATED LINES OF POSITION.
 INFUT FARAMETERS:
                       SIG1 AND SIG2- STANDARD ERRORS OF TWO LOP'S
TBETA - ANGLE OF INTERSECTION IN DEGREES
(0-180 DEG)
COR - CORRELATION COEFFICIENT
(USUALLY ZERO EXCEPT FOR HYPEFEC
OR SEXTANT POSITIONING)
                                                                                                                                        HYPEFECIIC
      OUTFUT PARAMETERS: SGX90 AND SGY90-
                                                                  - SEMI-MAJOR AND MINOR AXES
OF 90% ERROR ELLIPSE
- RADIUS OF 90% CONFIDENCE CIFCLE
- AREA CF 90% CONFIDENCE ELLIPSE
- AREA OF 90% CONFIDENCE CIRCLE
                       RACIUS
ELAR
                        CIRAR
C COMFUTE ECCENTRICITY OF ELLIFSE

C=SIGY/SIGX

C COMFUTE BURT'S K FACTOR BY LINEAR INTERPOLATION

IF ((C.LE.1.).AND.(C.GT.0.9)) THEN

B=1.0361*C+1.10987

ELSE IF ((C.LE.0.9).AND.(C.GT.0.8)) THE
                                                ((C.LE _ 0.9) .AND. (C.GT.0.8)) THEN
B=0.9475*C+1.18961
((C.IE.0.8) .AND. (C.GT.0.7)) THEN
B=0.8508*C+1.26697
((C.IE.0.7) .AND. (C.GT.0.6)) THEN
                           ELSE IF
```

Many variables exist when considering accuracy requirements for a hydrographic survey. In general, higher accuracy means more time, money, and effort. Azimuth-azimuth geometry is the most accurate method of positioning analyzed in this thesis. This method involves at least two people ashore and good ship-to-shore communications. Currently, NOS acquires these data manually, which minimizes the speed that the vessel can operate and adds to processing time. On the other hand, a survey using a medium-range system needs little shore support and the data acquisition is automated. Accuracy predictions help keep a balance between accuracy and effort. If the desired accuracy is attainable using a range-range system instead of an azimuth-azimuth system, then the choice is otvious.

Hydrographic positioning in the future will be dominated ty two methods. For cffshore surveys, the Global Positioning System (GFS) is expected to give positional accuracy to 10 meters or better. GPS is a satellite positioning system currently being deployed by the Department of Defense and will provide near worldwide coverage for users. Since the full constellation of 18 satellites will not be operational until 1988, it is not yet known if the expected accuracy of 10 meters will be met. Nearshore surveys may use multiple LOP's for establishing hydrographic positions. The principle of least squares is applied to redundant cbservations yielding the most probable position. For both GPS and least squares positioning, confidence ellipses and circles can be determined, although the techniques involved are much more complicated than those presented in this thesis.

The accuracy classification scheme presented in this thesis is predicated on the elimination of systematic errors. Much work is needed in identifying the sources of systematic errors associated with hydrographic positioning equipment.

lengthened. In an investigation such as this, it is advisable to be conservative and use the maximum length of line which is operationally feasible to provide coverage of an area as large as possible. The radius of the 90 percent confidence circle gives the hydrographer a rough figure for answering the question: Does the submerged pile exist?

Knowing the parameters of the error ellipse could be useful for conducting wire-drag, wire-sweep, and side scar sonar operations. For a position obtained with low precision positioning equipment, the search to relocate a submerced feature could cover a large area. Knowing the parameters of the error ellipse could reduce the area, time, and effort of the search. The search pattern could be planned to cover the desired confidence ellipse.

With the quantification of accuracy, a decision must be made concerning how much confidence is needed to delete a certain feature from the chart after a search has been made. The 90 percent confidence level may be too low, whereas the 95 or 99 percent level may suffice. A balance must be maintained between confidence of disproval and time and effort spent on the search.

Accuracy predictions in the form of reliability contours can be displayed using computer graphic terminals. These displays will contribute to the efficient planning of surveys to meet specifications. Given the survey area, the available control, the positioning methods, and the precision of the positioning equipment, the hydrographer can plan the accuracy of the survey before it is conducted. The survey area and the available control may be such that there is flexibility to change control stations to optimize accuracy over an area of critical importance. This information can be displayed graphically and plans for the survey can be made accordingly. Likewise, given an accuracy limit, such as a 10-meter radius of the 90 percent confidence circle, the area to be covered at that accuracy can be maximized.

B. USES FOR ACCURACY FIGURES

NCS is currently developing the Shipboard Data System III (SDS III), a hydrographic data acquisition and processing system which will replace the present HYDROLCG/HYDRCFLOT system. SDS III will revolutionize data acquisition and processing techniques with the capability to perform high-speed calculations and display color graphics. With this increased computer potential, data manipulations—such as accuracy computations—can be performed.

Each position in a survey can be given a quality figure based on the radius of the 90 percent confidence circle. This figure is sufficient for non-critical positions of ordinary hydrographic data. Critical positions are those which are determined for significant features (i.e., wrecks, least depths, rocks, and other potential hazards). For these positions, the parameters of the 90 percent error ellipse can be computed, as well as the radius of the 90 percent confidence circle.

Many schemes can be envisioned for the use of an accuracy figure. For example, suppose the position of a submerced pile was determined by range-azimuth geometry in a prior survey. The radius of the 90 percent confidence circle is then 5.1 meters (Ex. 2, Ch. II). The charting agency now wishes to relocate the pile to determine if it still exists and is still a hazard to navigation. In low water visibility, a common technique used to resolve such an item would be to send divers down over the reported position and conduct a circle search. One diver remains at the reported position, holding a line, while the other diver swims a circumference holding the other end of the line. Theoretically, if the line is about 5 meters long and a hang does not occur, it is 90 percent certain that the pile has been removed. For a higher confidence, the line is

TABLE IX						
accuracy Pigures for $\sigma_1 = \sigma_2 = 3$ m, $\sigma_2 = 0$						
Angle of Inter.	К о _ж	K σ У	Radius of 90% Circ.	Area of Ellipse	Area cf Circle	
(d € g)	(31)	(2)	(m)	(sq m)	(sq m)	
98877 66554 4 777 227 1	471595198931602924 66777789901357164224 11111122350	900764210988776666	455792507458732811 6566677889011112248	11111111111111111111111111111111111111	015190990000000000000000000000000000000	

		T	BLE I		
lo	curacy i	rigures for	. g = g =	= 10 m, ρ	= 0
Angle of Inter.	Κσ x	Koy	Radius of 90% Circ.	Area of Ellipse	Area of Circle
(d€g)	(m)	(m)	(m)	(sq m)	(sq m)
9887766058443772211 = -	1.23-4-80 2.561-4-31-9 £ 222222233334555781647	10000000000000000000000000000000000000	5.68mggqx895956m4479 111127775681495479956 22222222222237334568976	729806169612430020 456949768452923930 444455678025842596	11111111111111111111111111111111111111

figures as a function of β for uncorrelated LOP's have been compiled using standard errors of 1.3 meters for azimuth-azimuth (Table VIII), 3.0 meters for range-range short-range (Table IX), and 10 meters for range-range medium-range (Table X) positioning systems.

Accuracy Figures for $\sigma_1 = \sigma_2 = 1.3$ m, $\sigma_2 = 0$ Angle of K σ_2 K σ_3 Radius of Area of Area of Inter. x y 90% Circ. Ellipse Circle (deg) (m) (m) (m) (sq m) (sq m) 90 2.8 2.8 2.8 2.5	TABLE VIII							
(deg) (m) (m) (sq m) (sq m)	Acci	uracy Fig			1.3 m, o			
	Angle of Inter.	^K σx	Kσy	Radius of 90% Circ.	Area of Ellipse	Area of Circle		
90 2.8 2.8 2.4 2.5 2	(deg)	(m)	(m)	(m)	(sq m)	(sq m)		
30 7.6 2.0 5.9 49 110 25 9.1 2.0 7.1 58 156 20 11.4 2.0 8.8 71 241 15 15.1 2.0 11.6 94 425 10 22.6 2.0 17.4 141 949 5 45.2 2.0 34.7 281 3,781	988776655544372211 98877665544372211	912479711866141 233333345555679115	2.1 2.1 2.0	888901958151918647 2222235578174	455567802583981411 222222333334457948 128	425 949		

However, as mentioned for 1:10,000-scale surveys in a range-range mode ($\sigma = 3$ meters), this rule does not always hold. On the other hand, it is possible to have β 's of less than 30° and still meet specifications. For example, azimuth-azimuth positioning can theoretically be used for β 's of 18° to 162° for a 1:10,000-scale survey. However, the eccentricity of the error ellipse is so small that the distortion introduced by using confidence circles can become misleading. In view of this, eccentricities of less that 0.2 should not be used.

Using the 90 percent radius criterion, a table has been assembled illustrating the β limit for various positioning geometries at different survey scales, using assumed standard errors (Table VII). The information in Table VII illustrates that the 30° to 150° β limit need not be fixed. The β limits should vary based on the scale of the survey and the precision of the positioning equipment. Accuracy

TABLE VII β Limits for Surveys							
Survey Scale	90% Radius	R-R β(σ = 3) β Limit	$R-R$ $(\sigma = 10)$ β Limit	Az-Az (σ = 1.3) β Limit			
1:2,500 1:5,000 1:10,000 1:20,000 1:40,000	(m) 2.5 5.0 10.0 20.0 40.0	(deg) 42-138 27-153 23-157*	(deg)	(deg) 35-145 23-157* 23-157* 23-157*			
* Fccentricity limit of 0.2 Note: 90% radii of all range-azimuth positions are assumed to be 5.1 meters for $\sigma = 3$ and $\sigma = 1.3$.							

AZIMUTH-AZIMUTH ACCURACIES (CONTINUED)

Fix	X	Y	Angle of	Radius cf
No-	<u>Coordinate</u>	Ccordinate	Intersection	90% Circle
23456789012567890125 888888889999999990000	2074992732814605033003110.8952732814460503330011.124280605033300311.124280605033300311.12428060503330033003311.12428060503330033	94636029498543920835 1548614029498543920835 15486140498543920837 15488626398877756699887765475669988776547756699887765	91.0 947.0 947.0 1004.3 1004.3 1100.8 1113.8 113.8 113.8 113.8 113.8 113.8 113.	888889901131110099888 22222223333333333222222

CLASSIFIED RANGE-AZIMUTH POSITIONS

Control Stations: MESSEL 1932 occupied, initial USE MCN 1978 Standard Errors: Range--3 meters; T-2--1.3 meters

Fix No.	<u>Cocrdinate</u>		Angle of Intersection	Radius cf 90% Circle
######################################	809608372781276305438982609041102788529590902879583748049972 54629554216661496942708071528675577834577990592966950160632 897752945884113923471575486386894843209697711644991345782279802 897070991110998778889900006991070900112110001122836752798116 89070991110998778889900006991070900112711000112283675272211000122 223232322333333322222223333333333	9174578929506182634111435678467846645148929999557206075724410 9340163987621749656105799787289263558831164468243346887666129 13261880799311099091084631998875759388090195368237454604683685 1844163888892320262308533570479285532247825888027666902470427896 64432098834578900998990109880998887801098876788016789098776665567	00000000000000000000000000000000000000	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,

RANGE-AZIMUTH ACCURACIES (CONTINUED)

Fix	X <u>Coordinate</u>	Y Coordinate	Angle of Intersection	Radius of 90% Circl∈
689012345678901234 7778888888888999999	33333333333333333333333333333333333333	393.376.50 397.376.50 397.37776.50 398.666.297776.50 398.6663.78.35.75.40 399.55.	999999999999999999999999999999999999999	11111111111111111111111111111111111111
495 496 497	3197.78 3161.00	3504.04 3465.96	90.0 90.0	5. 1 5. 1

APPENDIX C

PROGRAM FOR 90 PERCENT CONFIDENCE ELLIPSE PARAMETERS

```
PROGFAM NAME: ELLIF
   DESCRIPTION: COMPUTES ORIENTATION, 90% SIGMA-X, 90% SIGMA-Y, FCR ELEGR ELLIPSE ABOUT A HYDROGRAPHIC POSITION ESTABLISHED BY RANGE-RANGE, AZIMUTH-AZIMUTE OR RANGE-AZIMUTH POSITION
   AUTHOR: NICHOLAS E. PERUGINI
LT. NO AA
NAVAL POSTGFADUATE SCHOOL
CCCCCC
    DATE:
                   SEPTEMBER , 1984
            IMPLICIT REAL * 4 (A-H,C-Z)
LUES: FOR RANGE-RANGE AND AZIMUTH-AZIMUTH:
-XL AND YL ARE COORDINATES OF LEFT STATION
-XR AND YR ARE COORDINATES OF RIGHT STATION
-SIGI AND SIGR ARE RESPECTIVE STANDARD ELFO
ASSCCIATED WITH EACH LOP
      INITIALIZE VALUES:
                           FOR FANGE-AZIMUTH:
-XL AND YL ARE CCORDINATES OF OCCUPIED STATION
-SIGL IS SIGMA OF THEODOLITE LOP
-SIGR IS SIGMA OF RANGE LOP
            XL=4914.75
YI=2009.86
SIGL=3.0
C
            XR=2474.75
YR=4247.42
SIGR= 3.0
   ENTER CORRELATION CCEFFICIENT: USUALLY ZERO FOR R-F,
                                                                 R-AZ, AND AZ-AZ
            RC = 0.0
            PI=3.141593
C EN
   IND=1
C***********
   INC IS A TOGGLE WHICH CHECKS FOR BETA GREATER THAN 90 DEG. NOTHING IN PROGRAM SHOULD BE CHANGED FROM HERE ON
   READ IN DATA FROM LATA FILE: IFIX = FIX NUMBER

EX = X COORDINATE OF HYDRO POSITION

EY = Y COORDINATE OF HYDRO POSITION

TD = ANGLE OF INTERSECTION IN DEGREES

SENTINEL IS IFIX = 999, TELLS PROGRAM TO STOP READING
    10
              CCNTINUE
```

```
REAC (4,20) IFIX.ILL.PX.FY.TD.RAD

FCRMAT (1X,13,3X,11,6X,F7.2,6X,F7.2,5X,F8.4,3X,F5.2)

INC = 0

IF (IFIX.EQ.999) GO TO 900

IF (ID.LT.90.) ED=ID

IF (ID.LT.90.) GO TO 30

WITH BETA LESS THAN 90 DEGREES: TOGGLE TURNED CN TO

DF=180.-TD
      20
                                                     30
90 DEGREES: TOGGLE TURNED ON TO ONE
               DE=180.-TD
30
C
C
C
               INC=1
               CCNTINUE
           P TANGENT FUNCTION FROM GCING UNDEFINED IN A RARE CASE THE FIX AND CONTROL STATION HAVING SAME COORDINATES IF (FX.EQ.XL) FX=PX+ 0.5 IF (FY.EQ.YL) FY=PY+ 0.5
    CHANGE DEGREES TO RADIANS
BETA=.01745325*DD
USE LEFT STATION AS BASIS FOR COMPUTATIONS
ORIENTATION ANGLES WILL BE FIXED WITH RESPECT TO LEFT LOP
     FINE AZIMUTH FROM NCRTH BETWEEN HYDRO POSITION AND LEFT STATICN. AZIMUTH WILL BE DEFINED BETWEEN 0-180 DEGREES MEASURED CLOCKWISE FROM NORTH.

THIS IS THE RANGE-RANGE AZIMUTH DETERMINATION.

IF (INC. NE. 1) GC TO 40

IF (PY.GE.YL) THEN

IF (PY.GE.XL) THEN
                                  ALPHA = PI-ATAN((PY-YL)/(PX-XL))
                                  ALPHA = ATAN((PY-YL)/(XL-PX))
                         END IF
               EISE
                         IP (PX.GE.XL) THEN
ALPHA = ATAN ((YL-PY)/(PX-XL))
                                  ALFPA = PI-ATAN((YL-PY)/(XL-PX))
   END IF
GC TO 60
AZIMUTH FIXING FOR AZIMUTH-AZIMUTH POSITIONS
40 CCNTINUE
               IF (FY.GE.YL) THEN
IF (PX.GE.XL) THEN
ALPHA = ATAN ((PX-XL)/(PY-YL))
                                 ALPHA = II-ATAN((XL-PX)/(PY-YL))
                         END IF
               ELSE
                         IF (PX.GE.XL) THEN
ALPHA = PI-ATAN ((PX-XL)/(YL-PY))
                         ALPHA = ATAN((XL-PX)/(YL-PY))
END IF
               END IF
        AZIMUTH EQUALS THETA FOR RANGE AZIMUTH CASE, ASSUMING THEODOLITE SIGMA IS LESS THAN RANGE SIGMA
              1F (IND.EQ.3) GC TO 70
  COCO
     BEGIN COMPUTING THETA, THAT IS THE ANGLE OF ROTATION FROM
     LEFT LCP
CONTINUE
               P1=SIGL**2*SIN(2*BETA)+2*RO*SIGL*SIGR*SIN(BETA)
```

APPENDIX D ACCURACY CLASSIFICATION: 90 PERCENT CONFIDENCE ELLIPSES

CLASSIFIED RANGE-RANGE POSITIONS

Control Stations: BFACH LAB 1982 and MUSSEL 1932

Standard Error Used in Computations: 3 meters

Fix	X	Y	Beta	90%	90%	Orienta-
No.	Coord.	Coord.		<u>Sigma X</u>	<u>Sigma Y</u>	<u>tion</u>
1234567890123456789012345678901234567890	5187666061333215744751866458983727278376 005220410661333215744751866458983727278376 82108034528114037374467305979252747356 680086578019745579992605079108678024564736 68008657801974557909260431086780245642087 200372222237242222237222237372222223373333333222	7954536737352913176504306851177526977802 264817313463260836574962709373379793053883 276481725346669558739985417081256193153108 9011087881230076890167890100975379012565280 9011087881241444455554444444555594444	06603944607400078298253918178924003177771 7187060175248746210830987678265456542113 2211122321111111111111111111111111	2397129385248277210930987678265456543223	12332102345431235555555555555555555555555555555	0326311029572978255847330728473626273546 9500584271494563935959360638361592629518 78998778899887788999788990998889990009998

CLASSIFIED AZIMUTH-AZIMUTH POSITIONS
Control Stations: USE MON 1978 and MUSSEL 1932
Standard Error Used in Computations: 1.3 meters

Fix	X	Y	Beta	90%	90%	Orienta-
No.	Ccord.	Coord.		<u>Sigma X</u>	<u>Sigma Y</u>	<u>tion</u>
9012345678123456789012345678901234567890 12222222333333333344444444555555555556 6666666666	2615202111750382578905708794038780738009 28464653739975142752059967523537439738009 97790064848772347467752660433050818024204 43211976433322222298765456689047913701129 44444933573322222298765456689047913444555545	4976044241582390969366825126089763106335 17762449121097268638062088375074222234587109726863806208251222439097686380622543210123455567890 2222233333333333333333333333333333333	906243925717890380041956418781122964019263963186305826159628518877149405174179554444333333445555554444333333445555554444333332211103	987665555455667919876655556786554444333355	00011111121111000000111111111011120334441	4&&&&C16Cmin4&1km1791190inkwn&9iin4074CkknnC 999999988767788887899888i667778888877776541 9mmnammammammammammammammammammammammamma

CLASSIFIED RANGE-AZIMUTH POSITIONS

Control Stations: USE MON 1978, MUSSEL 1932

Standard Errors: RANGE--3 meters; T-2--1.3

Fix	Ccord.	Coord.	Зеtа <u>s</u>	90% igma X	90% <u>Sigma Y</u>	Orienta- tion
44444444444444444444444444444444444444	8096083727812763054389826090411027885295 5462955421666149694270807152867557834577 8975294588413923471575486386894843209697 8976999110699877888990000000000000000000000000000	917457892950618263411114356784667846645148 9340163987621749656105799787289263558831 1326188075331109909108463159887575938809901 6432098345789009989901084631598887980109887 644320983345789009989990109888098888098887 64432098345789009989990109888098888780109887	000000000000000000000000000000000000000	00000000000000000000000000000000000000	**************************************	7900646000000000000000000000000000000000

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